

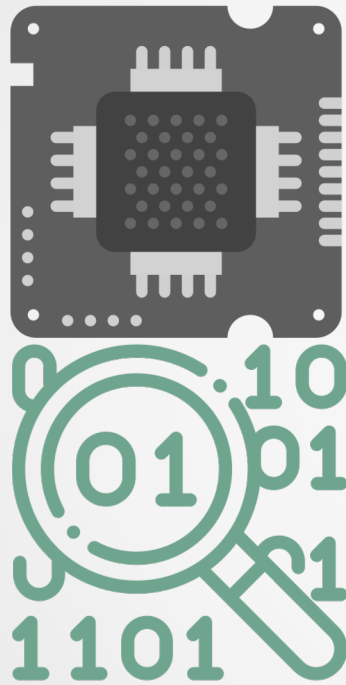
Analyzing Semantic Correctness with Symbolic Execution: A Case Study on PKCS#1 v1.5 Signature Verification

Sze Yiu Chau
Purdue University

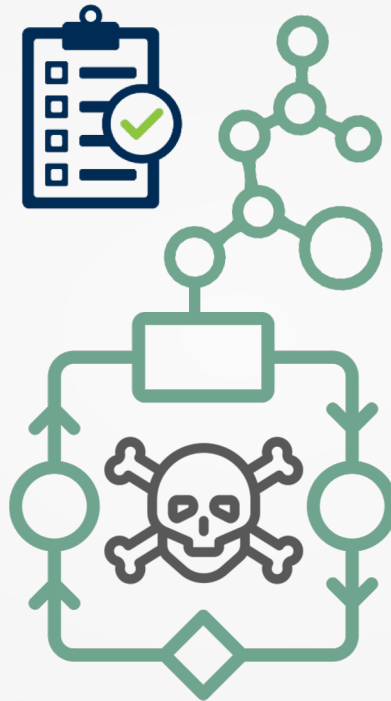
Joint work with Moosa Yahyazadeh, Omar Chowdhury,
Aniket Kate, Ninghui Li



Software Testing



Low-level
Errors



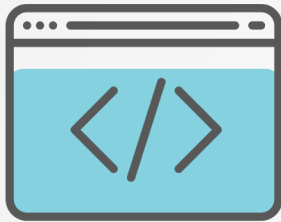
Logical Errors



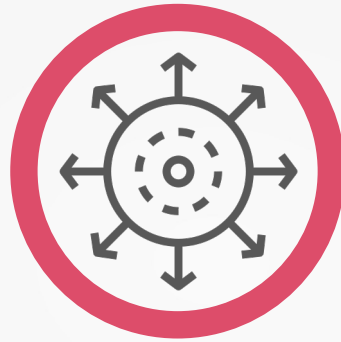
Attacks
e.g. libssh auth. bypass,
crypto. attacks

This work

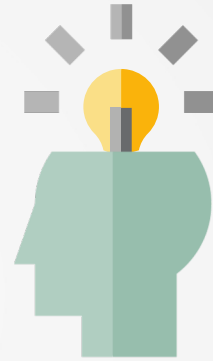
- Symbolic execution for analyzing semantic correctness



Code
Coverage



Scalability
Challenges

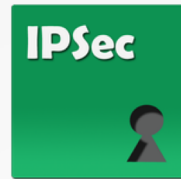
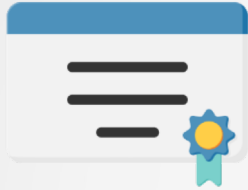


Domain
Knowledge

- Case study: Implementing PKCS#1 v1.5 signature verification

Motivation

- PKCS#1 v1.5 RSA signature is widely used



- **Previous work on X.509 testing neglect to analyze RSA signature verifications**
(Brubaker et al. 2014, Chen et al. 2015, Chau et al. 2017)

Motivation

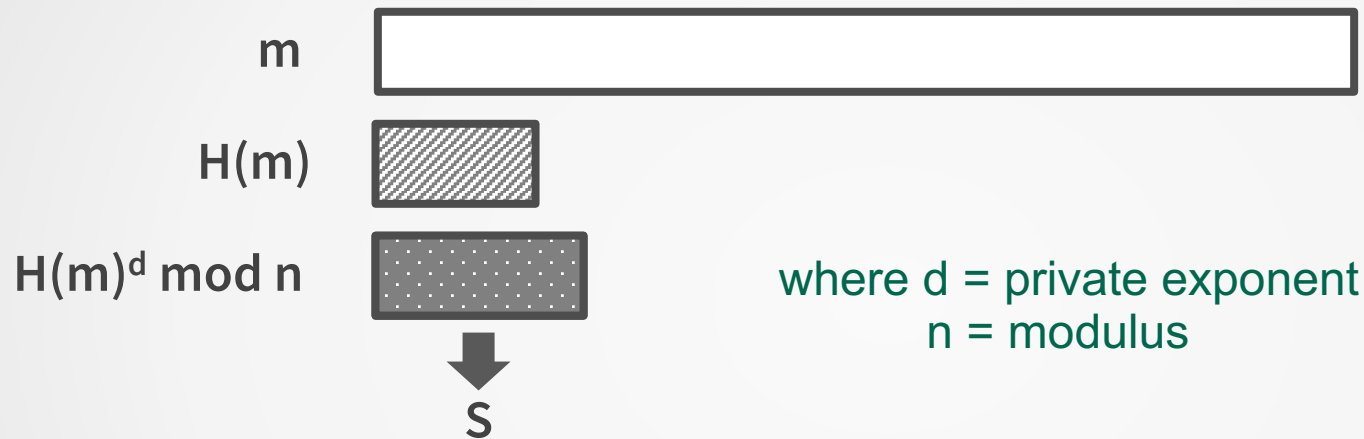
- Implementations need to verify signatures robustly
- Logical errors may allow **signature forgery**
- e.g. Bleichenbacher 2006, Kühn et al. 2008



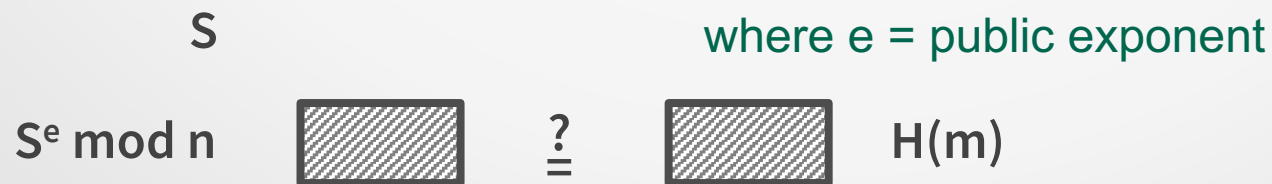
Textbook RSA signature



- Signing message m :



- Given (S, m, e, n) , verifying S is a valid signature of m



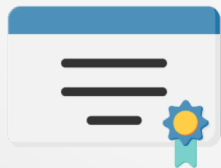
Beyond textbook RSA

- **Reality is more complex than that**
 1. Which $H()$ to use?
 - SHA-1, SHA-2 family, SHA-3 family ...
 2. n is usually much longer than $H(m)$
 - $|n| \geq 2048\text{-bit}$
 - $|\text{SHA-1}| = 160\text{-bit}$, $|\text{SHA-256}| = 256\text{-bit}$
- **Need padding and meta-data**



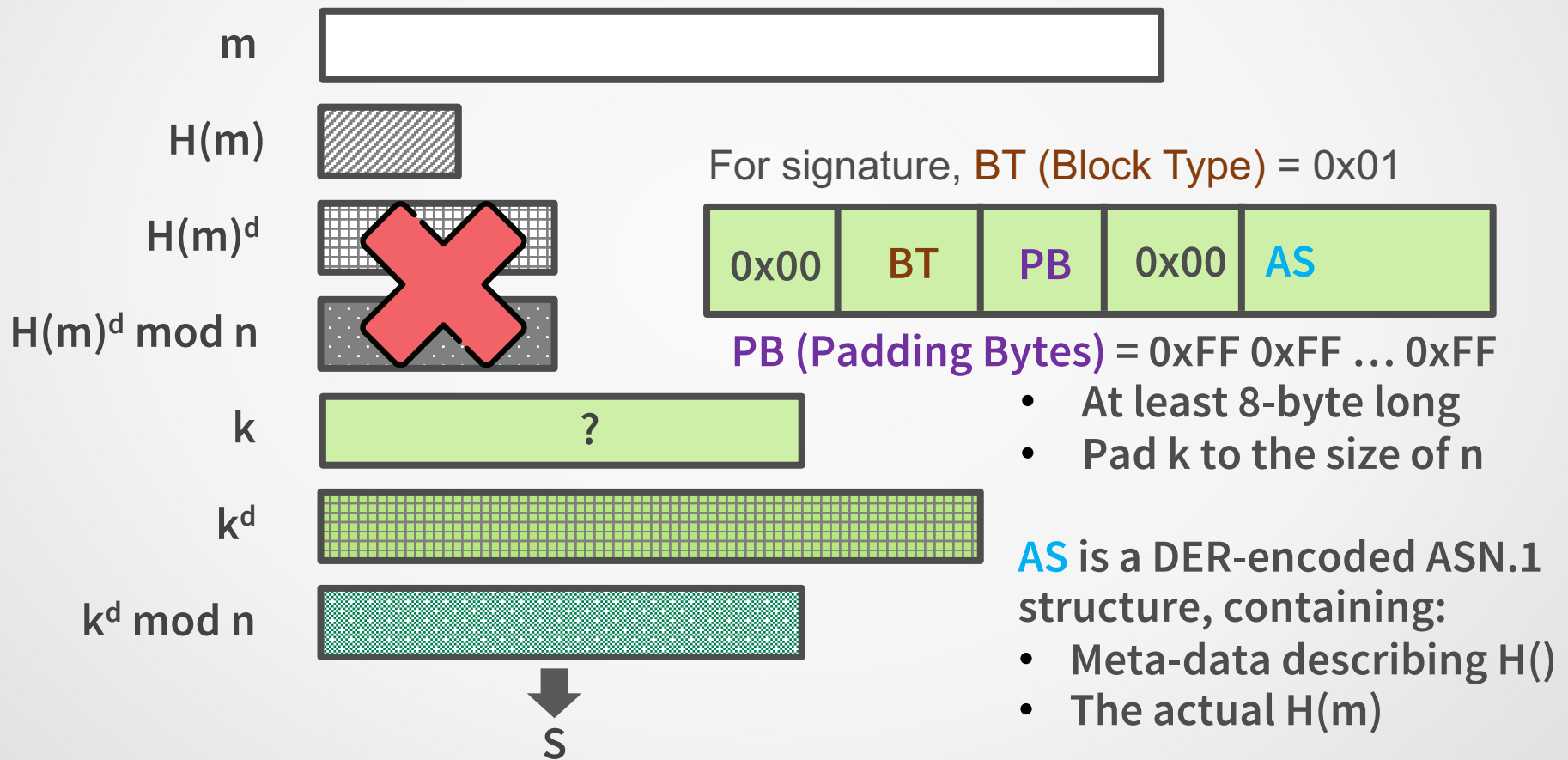
Beyond textbook RSA

- The PKCS#1 family of standards
 - Published by RSA (the company)
 - Both encryption and signature schemes
 - version 2+ adapted schemes from Bellare et al.
 - For signatures, **version 1.5 most widely used**
 - e.g. certificates of Google, Wikipedia



PKCS#1 v1.5 Signature Scheme

- Signing:



PKCS#1 v1.5 Signature Scheme

- DER encoded object is a tree of <T,L,V> triplets
- **AS** looks like this when encoded:

```
/** all numbers below are hexadecimals **/  
/* [AS.DigestInfo] */  
30 w // ASN.1 SEQUENCE, length = w = 0x21  
  /* [AlgorithmIdentifier] */  
  30 x // ASN.1 SEQUENCE, length = x = 0x09  
    06 u 2B 0E 03 02 1A // ASN.1 OID, length = u = 0x05  
    05 y // ASN.1 NULL parameter, length = y = 0x00  
  /* [Digest] */  
  04 z // ASN.1 OCTET STRING, length = z = 0x14  
    /* H(m), H()=SHA-1(), m = "hello world" */  
    2A AE 6C 35 C9 4F CF B4 15 DB  
    E9 5F 40 8B 9C E9 1E E8 46 ED
```

- altogether 35 bytes if $H() = \text{SHA-1}()$

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PKCS#1 v1.5 Signature Scheme

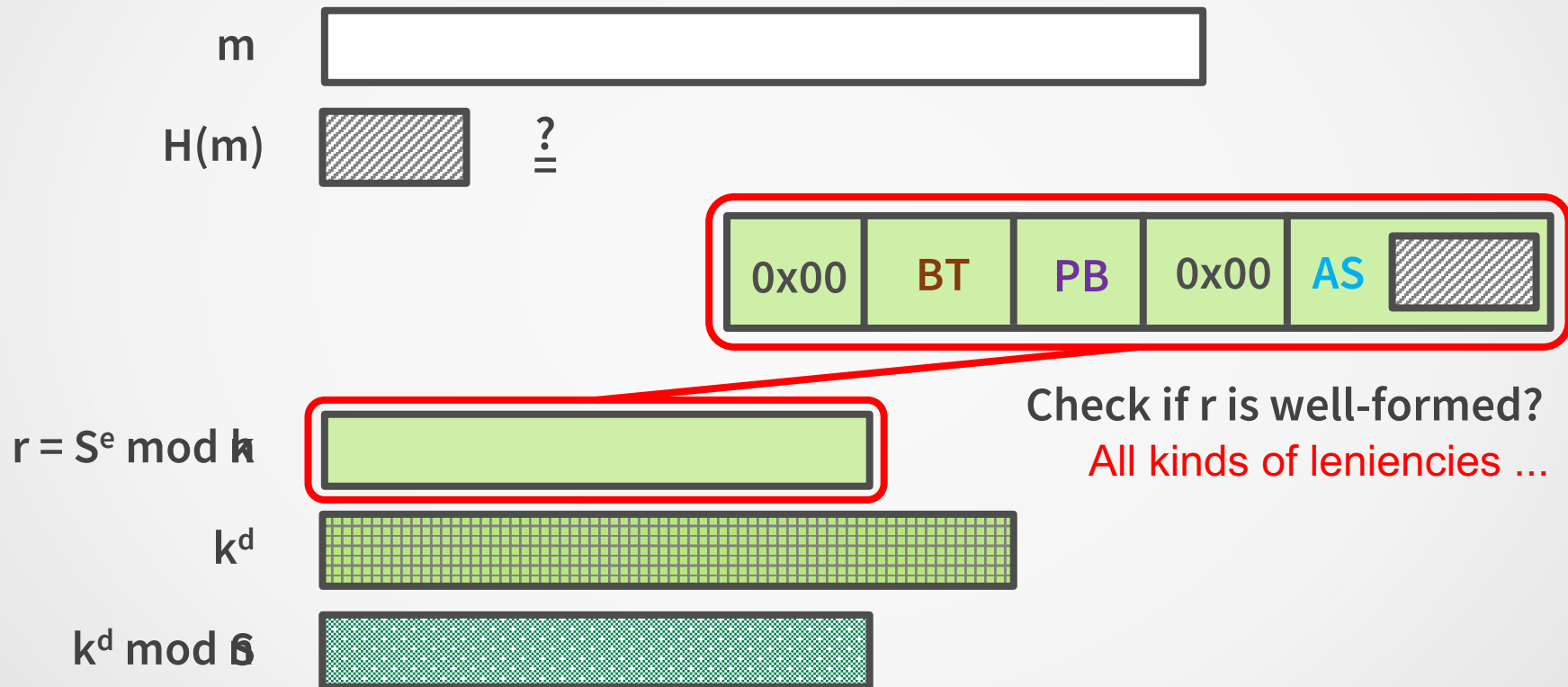
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PKCS#1 v1.5 Signature Scheme

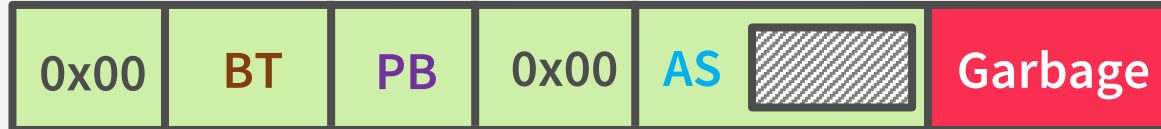
- Given (S, m, e, n) , verifier computes $H(m)$ and $r = S^e \bmod n$



Bleichenbacher's low exponent attack

- Yet another crypto attack attributed to D. Bleichenbacher
- CRYPTO 2006 rump session
- Some implementations accept malformed r'

r'



- **Existential forgery possible** when e is small
- **Generate signatures** for arbitrary m **without** d



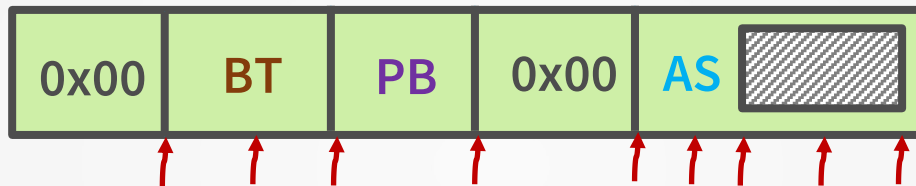
Bleichenbacher's low exponent attack

- A contributing factor to the push for bigger e (e.g. 65537)
- Smaller e more efficient for signature verifier
 - $e = 3$ prescribed in some protocols
 - (e.g. DNSSEC [RFC3110, Sect. 4])



Why was the attack possible?

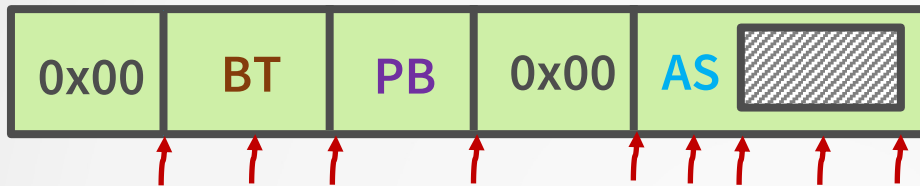
- Problem: accept malformed input w/ **GARBAGE** unchecked
- Can be in many different locations, not only at the end



- Longer modulus makes forgery easier
 - More **GARBAGE** bits to use
 - Can handle longer hashes / **slightly larger e**

To find these attacks

- Want to see how input bytes are being checked

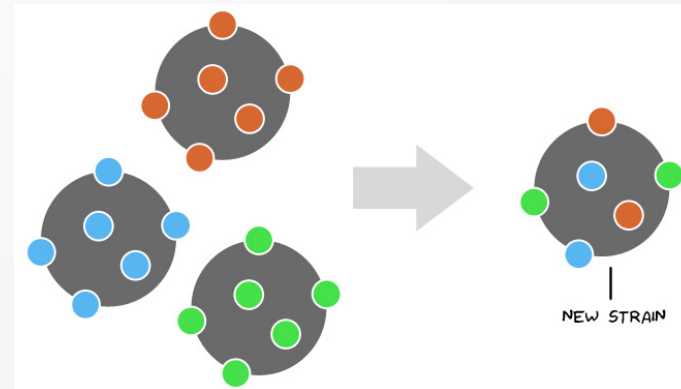
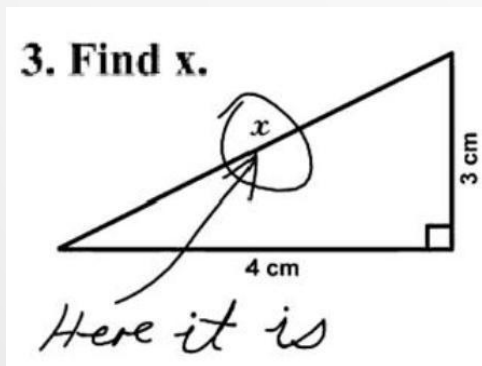


- If enough unchecked **GARBAGE** then



Automatically generate concolic test cases

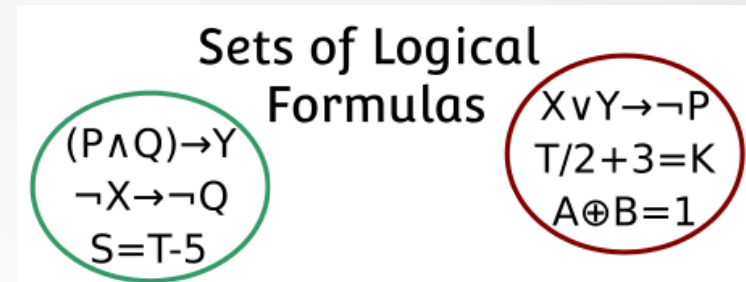
- **Observation: size of components exhibit linear relations**
- e.g. $\sum \text{length}(\text{components}) = |n|$; ASN.1 DER
- Programmatically capture such linear constraints
- Ask Symbolic Execution to find satisfiable solutions



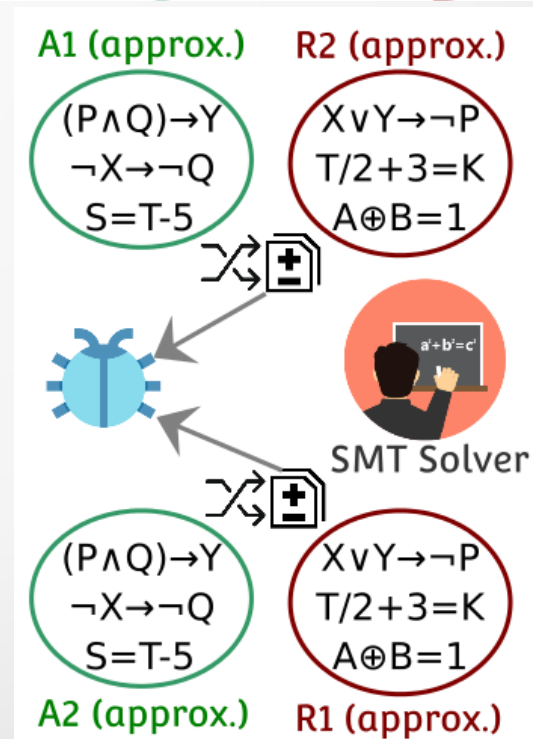
- Based on that, **automatically pack symbolic/concrete components** into test buffers

Testing with Symbolic Execution

- Symbolic Execution with concolic test cases

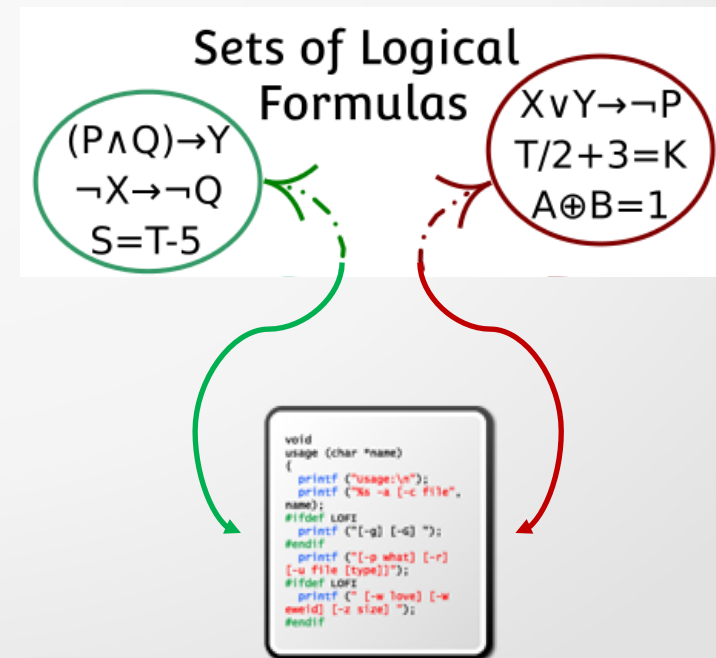


- Very useful abstraction
 - What and how things are being checked in code?
- Formulas can help cross-validate implementations



Finding root causes

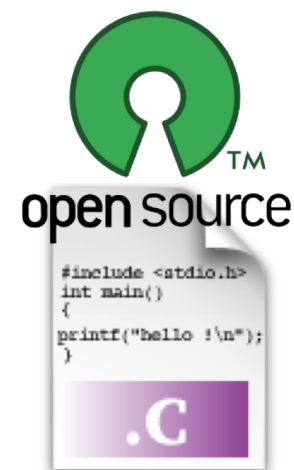
- **Locate the piece of code that imposes wrong constraints**
- Can we go from formula abstraction back to code?
- **Constraint Provenance Tracking**
 - Keep a mapping of <clause, source-level origin>
 - Tiny space & time overhead



Implementations Tested

Discussion of signature forgery assumes $e = 3$ and SHA-1, attacks also applicable to newer hash algorithms

<u>Name - Version</u>	<u>Overly lenient</u>	<u>Practical exploit under small e</u>
axTLS - 2.1.3	YES	YES
BearSSL - 0.4	No	-
BoringSSL - 3112	No	-
Dropbear SSH - 2017.75	No	-
GnuTLS - 3.5.12	No	-
LibreSSL - 2.5.4	No	-
libtomcrypt - 1.16	YES	YES
MatrixSSL - 3.9.1 (Certificate)	YES	No
MatrixSSL - 3.9.1 (CRL)	YES	No
mbedTLS - 2.4.2	YES	No
OpenSSH - 7.7	No	-
OpenSSL - 1.0.2l	No	-
Openswan - 2.6.50 *	YES	YES
PuTTY - 0.7	No	-
strongSwan - 5.6.3 *	YES	YES
wolfSSL - 3.11.0	No	-



* configured to use their own internal implementations of PKCS#1 v1.5

Leniency in Openswan 2.6.50

- Ignoring padding bytes (CVE-2018-15836)
- Simple oversight, severe implications
- **Exploitable** for signature forgery

```
/* check signature contents */
/* verify padding (not including
   any DER digest info! */
padlen = sig_len - 3 - hash_len;
...
/* skip padding */
if(s[0] != 0x00 || s[1] != 0x01
    || s[padlen+2] != 0x00)
{ return "3""SIG padding does not
s += padlen + 3;
```

- Use this r' `/** all numbers below are hexadecimals **/`

00	01	GARBAGE	00	30	21	04	16	SHA-1(m')
----	----	---------	----	----	----	-----	-----	----	----	-----------

- Want: $(a + b)^3 = a^3 + 3a^2b + 3b^2a + b^3$, s.t.



- MSBs of a^3 give what is before GARBAGE
- LSBs of b^3 give what is after GARBAGE
- LSBs of $a^3 + 3a^2b + 3b^2a +$ MSBs of b^3 stay in GARBAGE
- **fake signature** $S' = (a+b)$

New unit test in Openswan

xelerance / Openswan

Code

Issues 95

Pull requests 0

Projects 0

Wiki

Insights

wo#7449 . test case for Bleichenbacher-style signature forgery

Special thanks to Sze Yiu Chau of Purdue University (schau@purdue.edu) who reported the issue, and made major contributions towards defining this test case.

master (#330) v2.6.51.2 ... v2.6.50.1

 bartman committed on Aug 20

1 parent [9eaa6c2](#)

Showing 6 changed files with 218 additions and 0 deletions.

1 tests/unit/libopenswan/Makefile

	+	-	
		-23,6	+23,7
		clean check:	
23	23		@\${MAKE} -C lo04-verifypubkeys \$@
24	24		@\${MAKE} -C lo05-datatot \$@
25	25		@\${MAKE} -C lo06-verifybadsigs \$@
	26	+	@\${MAKE} -C lo07-bleichenbacher-attack \$@
26	27		

Leniency in strongSwan 5.6.3

1. Not checking AlgorithmParameter (CVE-2018-16152)

- classical flaw found in others like GnuTLS, Firefox years ago
- **Exploitable** for signature forgery
- hide **GARBAGE** in **AlgorithmParameter**
- follow the Openswan attack algorithm
 - adjust what a^3 and b^3 represent, **fake signature** $S' = (a+b)$



Leniency in strongSwan 5.6.3

2. Accept trailing bytes after Algorithm OID (CVE-2018-16151)

- interestingly, **Algorithm OID** is not matched exactly
- a variant of longest prefix match

```
/* [AlgorithmIdentifier] */
30 09
06 05 2B 0E 03 02 1A
05 00






/* [AlgorithmIdentifier] */
30 0C
06 08 2B 0E 03 02 1A AB CD EF
05 00
```

both would be recognized as OID of SHA-1

- knowing this, one can hide **GARBAGE** there
- follow the Openswan attack algorithm
- adjust what a^3 and b^3 represent, **fake signature** $S' = (a+b)$



strongSwan Security Update

<input checked="" type="checkbox"/>	 StrongSwan daemon starter and configuration file parser	742 kB
<input checked="" type="checkbox"/>	 StrongSwan Internet Key Exchange daemon	56 kB
<input checked="" type="checkbox"/>	 StrongSwan utility and crypto library	1.4 MB
<input checked="" type="checkbox"/>	 StrongSwan utility and crypto library (standard plugins)	267 kB
<input checked="" type="checkbox"/>	 Virtual Linux kernel tools	3 kB

▼ Technical description

Changes

Description

- [CVE-2018-17540](#)

Version 5.3.5-1ubuntu3.7:

* SECURITY UPDATE: Insufficient input validation in gmp plugin

- debian/patches/strongswan-5.3.1-5.6.0_gmp-pkcs1-verify.patch: don't parse PKCS1 v1.5 RSA signatures to verify them in
src/libstrongswan/plugins/gmp/gmp_rsa_private_key.c,
src/libstrongswan/plugins/gmp/gmp_rsa_public_key.c.

- [CVE-2018-16151](#)

- [CVE-2018-16152](#)

* SECURITY UPDATE: remote denial of service

Some key generation programs still forces $e = 3$

e.g., ipsec_rsasigkey on Ubuntu

NAME

```
ipsec_rsasigkey - generate RSA signature key
```

SYNOPSIS

```
ipsec rsasigkey [--verbose] [--seeddev device] [--seed numbits] [--nssdir nssdir]  
                [--password nssppassword] [--hostname hostname] [nbits]
```

DESCRIPTION

rsasigkey generates an RSA public/private key pair, suitable for digital signatures, of (exactly) nbits bits (that is, two primes each of exactly nbits/2 bits, and related numbers) and emits it on standard output as ASCII (mostly hex) data. nbits must be a multiple of 16.

The public exponent is forced to the value 3, which has important speed advantages for signature checking. Beware that the resulting keys have known weaknesses as encryption keys and should not be used for that purpose.

Leniency in axTLS 2.1.3

1. **Accepting trailing GARBAGE (CVE-2018-16150)**
 - original Bleichenbacher '06 forgery also works



Leniency in axTLS 2.1.3

2. Ignoring AS.AlgorithmIdentifier (CVE-2018-16253)

```
/** all numbers below are hexadecimals **/  
/* [AS.DigestInfo] */  
30 21  
/* [AlgorithmIdentifier] */  
30 09  
06 05 2B 0E 03 02 1A  
05 00  
/* [Digest] */  
04 14  
/* H(m), H()=SHA-1(), m = "hello world" */  
2A AE 6C 35 C9 4F CF B4 15 DB  
E9 5F 40 8B 9C E9 1E E8 46 ED
```

this whole chunk
is skipped ...

```
if (asn1_next_obj(asn1_sig, &offset,  
ASN1_SEQUENCE) < 0 ||  
asn1_skip_obj(asn1_sig, &offset,  
ASN1_SEQUENCE)) goto end_get_sig;  
  
if (asn1_sig[offset++] != ASN1_OCTET_STRING)  
goto end_get_sig;  
*len = get_asn1_length(asn1_sig, &offset);  
ptr = &asn1_sig[offset]; /* all ok */  
  
end_get_sig:  
return ptr;
```

- Probably because certificates have an explicit signature algorithm field, which gives H()

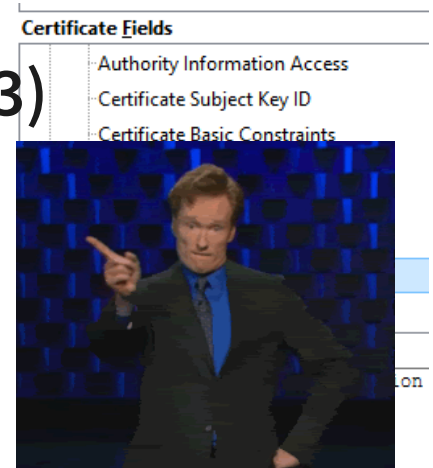
Certificate Fields	
Authority Information Access	
Certificate Subject Key ID	
Certificate Basic Constraints	
Certificate Authority Key Identifier	
Certificate Policies	
CRL Distribution Points	
Certificate Signature Algorithm	
Certificate Signature Value	

Field Value
PKCS #1 SHA-256 With RSA Encryption

Leniency in axTLS 2.1.3

2. Ignoring AS.AlgorithmIdentifier (CVE-2018-16253)

- Just because $H()$ is known from outside
- Doesn't mean it can be skipped



- Use this r' `/** all numbers below are hexadecimals **/`

```
00 01 FF FF FF FF FF FF FF FF 00  
30 5D 30 5B GARBAGE 04 16 SHA-1(m')
```



- hide **GARBAGE** in **AlgorithmIdentifier**
- follow the Openswan attack algorithm
 - adjust what a^3 and b^3 represent, **fake signature** $S' = (a+b)$

Leniency in axTLS 2.1.3

3. Trusting the declared ASN.1 DER lengths w/o sanity checks [CVE-2018-16149]

```
/** all numbers below are hexadecimals **/  
/* [AS.DigestInfo] */  
30 w  
  /* [AlgorithmIdentifier] */  
  30 x  
    06 u 2B 0E 03 02 1A  
    05 y  
  /* [Digest] */  
  04 z  
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```

put absurdly large values to trick verifier into reading from illegal addresses



- DoS PoC: making z exceptionally large **crashed the verifier**

patching axTLS (ESP8266 port)

igrr / axtls-8266

Code

Issues 8

Pull requests 1

Projects 0

Insights

Apply CVE fixes for X509 parsing

Apply patches developed by Sze Yiu which correct a vulnerability in X509 parsing. See CVE-2018-16150 and CVE-2018-16149 for more info.

master (#60)



earlephilhower authored and igrr committed on Oct 22

1 parent e634adf

Showing 2 changed files with 76 additions and 38 deletions.

12 ssl/os_port.h



```
@@ -142,6 +142,18 @@ static inline int strlen_P(const char *str) {
```

```
142     while (pgm_read_byte(str++)) cnt++;
```

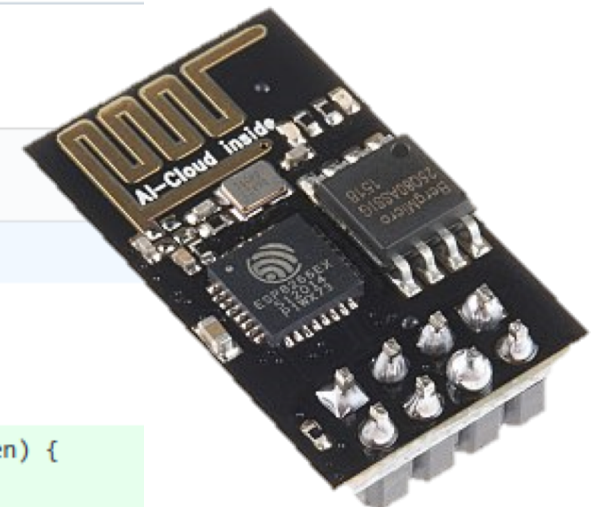
```
143     return cnt;
```

```
144 }
```

```
145 + static inline int memcmp_P(const void *a1, const void *b1, size_t len) {
```

```
146 +     const uint8_t* a = (const uint8_t*)(a1);
```

```
147 +     uint8_t* b = (uint8_t*)(b1);
```



Other leniencies

- Lax checks on ASN.1 DER lengths in MatrixSSL(CRL)

```
/** all numbers below are hexadecimals **/  
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30 w  
/* [AlgorithmIdentifier] */  
30 x  
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05 y  
/* [Digest] */  
04 z  
/* H(m), H()=SHA-1(), m = "hello world" */  
2A AE 6C 35 C9 4F CF B4 15 DB  
E9 5F 40 8B 9C E9 1E E8 46 ED
```

many possible values will be accepted

- Some bits in the middle of **AS** can take any values
- Doesn't seem to be numerous enough for practical attacks
- Variants of this leniency also found in *mbedTLS*, *libtomcrypt*, *MatrixSSL (Certificate)*

Leniency in MatrixSSL 3.9.1

MatrixSSL 4.x changelog

Changes between 4.0.0 and 4.0.1 [November 2018]

This version improves the security of RSA PKCS #1.5 signature verification and adds better support for run-time security configuration.

- Crypto:
 - Changed from a parsing-based to a comparison-based approach in DigestInfo validation when verifying RSA PKCS #1.5 signatures. There are no known practical attacks against the old code, but the comparison-based approach is theoretically more sound. Thanks to Sze Yiu Chau from Purdue University for pointing this out.
 - (MatrixSSL FIPS Edition only:) Fix DH key exchange when using DH parameter files containing optional privateValueLength argument.
 - psX509AuthenticateCert now uses the common psVerifySig API for signature verification. Previously, CRLs and certificates used different code paths for signature verification.

Conclusion

- RSA signature verification should be robust regardless of the **choice of e**
- Flawed verification can break authentication in different scenarios
- To analyze this, we extend symbolic execution with
 - Automatic generation of concolic test cases
 - Constraint Provenance Tracking
- Found new variants of Bleichenbacher '06 attacks after more than a decade, 6 new CVEs
- And many other unwarranted leniencies



Q&A

Thank You

Sze Yiu Chau

Computer Science, Purdue University

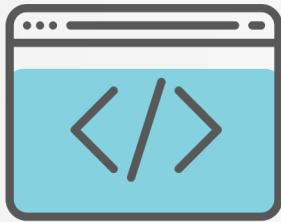
Email: schau@purdue.edu

Web: <https://www.cs.purdue.edu/homes/schau/>

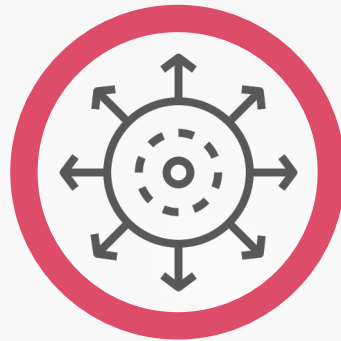
Additional Slides

This work

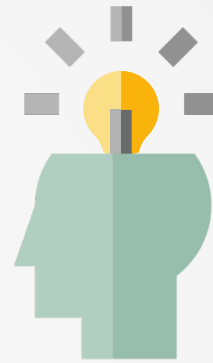
- Symbolic execution for analyzing semantic correctness



Code
Coverage



Scalability
Challenges



Domain
Knowledge

- Case study: Implementing PKCS#1 v1.5 signature verification
 - **Flaws** in TLS and crypto libraries, and IPsec software
 - Exploitable for **signature forgery and DoS** attacks



Bleichenbacher's low exponent attack

- $r' = 0x00 \parallel \text{BT} \parallel \text{PB} \parallel 0x00 \parallel \text{AS} \parallel \text{GARBAGE}$
- Assuming $e = 3$
- Construct $t = 00 \text{ 01 FF FF FF FF FF FF FF FF FF FF FF } 00 \parallel \text{AS} \parallel \text{FF .. FF}$
 - if $(\text{floor}(\sqrt[3]{t}))^3$ match r' before **GARBAGE** then
 - **fake signature** $S' = \text{floor}(\sqrt[3]{t})$
 - if necessarily, tweak m to get a different **AS**, try again



Bleichenbacher's low exponent attack

- $r' = 0x00 \parallel BT \parallel PB \parallel 0x00 \parallel AS \parallel \text{GARBAGE}$
- $= 00\ 01\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ 00 \parallel AS \parallel \text{GARBAGE}$
- assuming $e = 3$, $|n| = 1024$ bits, $r' < 2^{1009}$
 - want to find S' s.t. $S'^3 = r'$
- construct $t = 00\ 01\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ 00 \parallel AS \parallel FF\ ..\ FF$
- if $(\text{floor}(\sqrt[3]{t}))^3$ match r' before GARBAGE then we're done
 - fake signature $S' = \text{floor}(\sqrt[3]{t})$
- if necessarily, tweak m to get a different AS, try again

Bleichenbacher's low exponent attack

- $r' = 00\ 01\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ 00 \parallel AS \parallel GARBAGE$
- assuming $e = 3$, $|n| = 1024$ bits, $r' < 2^{1009}$
 - want to find S' s.t. $S'^3 = r'$
- distance between two consecutive perfect cubes:
 - $$b^3 - (b - 1)^3 = 3b^2 - 3b + 1 < 3 \cdot 2^{673} - 3 \cdot 2^{337} + 1$$
$$< 2^{675} \quad (\because b^3 < 2^{1009})$$
- assuming $H() = \text{SHA-1}()$, max length of GARBAGE is:
 - $1024/8 - (2 + 8 + 1 + 35) = 82$ bytes = 656 bits
- roughly 19 bits less than $b^3 - (b - 1)^3$, so around 2^{19} trials to find a working S'

Over-permissiveness in Openswan 2.6.50

- Use this r': `/** all numbers below are hexadecimals **/
00 01 GARBAGE 00 30 21 04 16 SHA-1(m')`
- Want: $(a + b)^3 = a^3 + 3a^2b + 3b^2a + b^3$
- Finding 'a' is similar to the original attack algorithm
- construct $t = 00\ 01\ 00\ 00\ ..\ 00$
 - compute $\alpha = \text{ceil}(\sqrt[3]{t})$
 - sequentially find the largest 'c' s.t. $((\alpha / 2^c + 1) 2^c)^3$ match r' before GARBAGE
 - then $a = (\alpha / 2^c + 1) 2^c$
 - this is to make as many LSBs of 'a' zeros
 - to avoid overlapping terms

Over-permissiveness in Openswan 2.6.50

- Use this r' : `/** all numbers below are hexadecimal */`
`00 01 GARBAGE 00 30 21 04 16 SHA-1(m')`
- Want: $(a + b)^3 = a^3 + 3a^2b + 3b^2a + b^3$
- Finding 'b' is a little more complex
- let $r_b = 00\ 30\ 21\ \dots\ \dots\ 04\ 16\ \text{SHA-1}(m')$, and $n' = 2^{|r_b|}$
 - r_b can be considered as $(b^3 \bmod n')$
 - since n' is a power of 2, $\phi(n') = 2^{|r_b|-1}$
 - we can guarantee r_b and n' are coprime w/ an odd $\text{SHA-1}(m')$
 - use Extended Euclidean Algorithm to find f , s.t.
 - $ef = 1 \pmod{2^{|r_b|-1}}$
that is, f is the multiplicative inverse of $e \bmod \phi(n')$
 - finally $b = r_b^f \bmod n'$

Leniency in strongSwan 5.6.3

3. Accepting less than 8 bytes of padding

- Can be used to make the other attacks easier
- Use no **padding**, gain more bytes for **GARBAGE**



Leniency in axTLS 2.1.3

2. Ignoring prefix bytes

```
i = 10;  
/* start at the first possible non-padded byte */  
while (block[i++] && i < sig_len);  
size = sig_len - i;  
/* get only the bit we want */  
if (size > 0) {... ..}
```

- First 10 bytes are not checked at all



Leniency in axTLS 2.1.3

2. Ignoring prefix bytes

- First 10 bytes directly skipped
- Make forgery easier, use this r' (first 90 bits are all zeros)

```
/** all numbers below are hexadecimals **/  
00 00 00 00 00 00 00 00 00 00 00 00  
30 21 ... .. 04 16 SHA-1(m') GARBAGE
```

- Reduce the distance between two consecutive perfect cubes
 - Easier to find S'



Leniency in axTLS 2.1.3

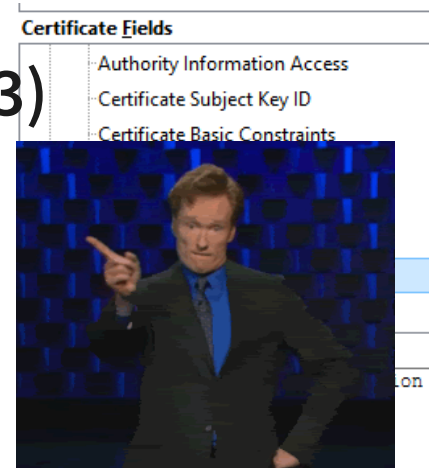
3. Ignoring AS.AlgorithmIdentifier (CVE-2018-16253)

- Just because $H()$ is known from outside
- Doesn't mean it does not need to be checked
- This can be exploit together with the previous 2 flaws

- Use this r'

```
/** all numbers below are hexadecimals **/  
00 00 00 00 00 00 00 00 00 00 00 00  
30 00 30 00 04 H().size H(m') GARBAGE++
```

- shorten the **AlgorithmIdentifier** to allow more **GARBAGE**
- useful with shorter modulus and longer hashes



Leniency in axTLS 2.1.3

4. Trusting the declared ASN.1 DER lengths w/o sanity checks [CVE-2018-16149]
 - DoS PoC: making z exceptionally large crashed the verifier
 - Particularly damaging
 - axTLS does certificate chain validation bottom-up
 - even if no **small e** in the wild
 - any MITM can inject a fake certificate with $e = 3$
 - **crash verifier** before the whole chain is verified against some trusted root anchors



Leniency in MatrixSSL 3.9.1 (CRL)

1. Mishandling Algorithm OID

```
/** all numbers below are hexadecimals */
/* [AS.DigestInfo] */
30 w
  /* [AlgorithmIdentifier] */
  30 x
    06 u 2B 0E 03 02 1A
    05 y
  /* [Digest] */
  04 z
    /* H(m), H()=SHA-1(), m = "hello world" */
    2A AE 6C 35 C9 4F CF B4 15 DB
    E9 5F 40 8B 9C E9 1E E8 46 ED
```

can take arbitrarily
any values

- Some bytes in the middle of **AS** can take any values
 - Depends on choice of H(), SHA-1: 5 bytes, SHA-256: 9 bytes
- Doesn't seem to be numerous enough for practical attacks

Discussion

- Parsing is hard!
- What robustness means depends on the context
 - Parser robustness (e.g. handling malformed inputs) is bad for security-critical scenarios
- Better way: construction-based verification
 - Many libraries have code for signing
 - for verifiers, instead of parsing, compute $H(m)$, prepare AS and construct r_v
 - then see if $r_v \equiv S^e \pmod n$