# LIRA: Lightweight Incentivized Routing for Anonymity

20th Annual Network & Distributed System Security Symposium February 27, 2013



Rob Jansen Aaron Johnson Paul Syverson U.S. Naval Research Laboratory Problem



**Onion Routers** 



**Onion Routers** 



**Onion Routers** 





#### Tor is Slow

#### Web (320 KiB)

#### Bulk (5 MiB)



# **Tor Utilization**

# ~3000 relays





### **Tor Utilization**



The Tor Project – https://metrics.torproject.org/

### Tor's Top 20 Exit Relays

Exit Probability	Advertised Bandwidth	Nickname	Country
7.25%	0.87%	chaoscomputerclub18	DE
6.35%	0.93%	chaoscomputerclub20	DE
5.92%	1.48%	herngaard	US
3.60%	0.66%	chomsky	NL
3.35%	1.17%	dorrisdeebrown	DE
3.32%	1.18%	bolobolo1	DE
3.26%	0.65%	rainbowwarrior	NL
2.32%	0.36%	sdnettor01	SE
2.23%	0.69%	TheSignul	RO
2.22%	0.41%	raskin	DE
2.05%	0.40%	bouazizi	DE
1.93%	0.65%	assk	SE
1.82%	0.39%	kramse	DK
1.67%	0.35%	BostonUCompSci	US
1.53%	0.40%	bach	DE
1.31%	0.73%	DFRI0	SE
1.26%	0.31%	Amunet2	US
1.13%	0.27%	Amunet8	US
0.84%	0.27%	chaoscomputerclub28	DE
0.76%	0.37%	DFRI3	SE
Total: 54.14%		cor	npass.torproject.org



# **Our Solution**

#### **Incentive Scheme**

LIRA

Relays' own traffic gets better performance

#### **Incentive Schemes**

- LIRA
- Gold star
- Tortoise
- BRAIDS
- Freedom
- PAR
- XPay

Relays' own traffic gets better performance

- Charge users, pay relays

### **Incentive Schemes**

	External payment	Non-relays pay	Efficiency concerns	Anonymity concerns
Freedom	*	*		
PAR	*	*		
XPay	*	*		
Gold star				*
Tortoise				*
BRAIDS			*	

# **Anonymous Incentives**





#### Problem: Priority identifies user as a relay

# **Anonymous Incentives**





# Problem: Priority identifies user as a relay Solutions

1. Give some priority "tickets" to all users (BRAIDS).

# Anonymous Incentives





Problem: Priority identifies user as a relay Solutions

- 1. Give some priority "tickets" to all users (BRAIDS).
- 2. Cryptographic lottery gives priority; winning tickets can be (secretly) bought (LIRA).

Bank





Bank gives anonymous coins to relays based on amount of traffic forwarded





Bank sets up lottery with each relay









Clients guess winners









# Cryptographic Lotteries

- Lottery at relay r $g_r: \{0,1\}^{2L} \rightarrow \{0,1\}^{2L}$ x wins if
  - $-g_r(x) = y_0 || y_1$  $-0 \le y_0 \oplus y_1$







# Cryptographic Lotteries

- Lottery at relay r $g_r$ : {0,1}<sup>2L</sup>  $\rightarrow$  {0,1}<sup>2L</sup> x wins if
  - $-g_r(x) = y_0 \parallel y_1$
  - $-0 \le y_0 \oplus y_1$



 g<sub>r</sub> defined from PRF f<sub>r</sub> using a Luby-Rackofflike construction

$$-y_0 = f_r(x_1) \oplus x_0$$
$$-y_1 = f_r(y_0) \oplus x_1$$

 $-g_r(x)=y_0\mid\mid y_1$ 

# Cryptographic Lotteries

- Lottery at relay r $g_r$ : {0,1}<sup>2L</sup>  $\rightarrow$  {0,1}<sup>2L</sup> x wins if
  - $-g_r(x) = y_0 \parallel y_1$
  - $-0 \le y_0 \oplus y_1$



- g<sub>r</sub> defined from PRF f<sub>r</sub> using a Luby-Rackofflike construction
  - $-y_0 = f_r(x_1) \oplus x_0$
  - $-y_1 = f_r(y_0) \oplus x_1$
  - $-g_r(x) = y_0 \parallel y_1$
- $f_r(x) = H(x(H(H(x) x_r^d)))$ 
  - H is a hash function
  - $-x_r$  is public; bank gives  $x_r^d$  to r during setup,
  - d is bank's private RSA key

Analysis

# Efficiency

		LIRA	BRAIDS	
Bank	Blind signatures/s	127.5+127.5f (256B/sig)	637.5 (488 B/sig)	
Relay	Priority verification	6 hashes (18 us)	PBS verify (1500 us)	
Normal Client	Tickets / connection	0	1	
	<i>f</i> is fraction of credit redeemed. Entire network is transferring 1700 MiB/s. Signature size: 1024 bits. Ticket size: 320 bits. Linux OpenSSL benchmarks on Intel Core2 Duo 2.67 GHz			

### Anonymity

 With m buyers and n guessers, the probability that a prioritized circuit source is a given buyer is

 $1 / (m + np^3)$ 

compared to 1/(m+n) without priority.

• Linked priority degrades anonymity exponentially to 1/*m*.

#### Performance

#### Web (320 KiB)

#### Bulk (5 MiB)



#### Performance, More Capacity

#### Web (320 KiB)

#### Bulk (5 MiB)

lira

5%(+7%)

15%(+17%) 5%(+96%)

15%(+384%)

200

150



#### Conclusion

- 1. Volunteer-run Tor network is overloaded.
- 2. LIRA provides incentives to contribute by rewards with better network performance.
- 3. LIRA is more efficient than previous schemes while maintaining anonymity.
- 4. Full-network experiments demonstrate better performance and scalability.

### **Buying winning tickets**

- Client chooses  $y_0$ ,  $y_1$ ,  $0 \le y_0 XOR y_1 < p2^L$
- Using using PRF protocol, client reverses Luby-Rackoff process to get  $g_r^{-1}(y_0 \parallel y_1)$ .

Client *c* and bank *B* evaluate  $f_r(x)$ 1. *C* sends  $a^e x_r^d$  to B, *a* random. 2. *B* returns  $abx_r^d$ , *b* random. 3. *c* sends *b* H(*x*) $x_r^d$  to *B*. 4. *B* returns H(H(*x*) $x_r^d$ ) to *c*. 5. *c* outputs  $f_r(x) = H(x H(H(x)x_r^d))$ .

#### **PRF** Protocol



- 1. Client sends tickets to each relay in circuit.
- 2. Relays evaluate tickets. Winners must have unseen PRF inputs. Neighbors sent results.
- 3. If ticket wins and neighbors report wins, circuit is prioritized for next β bytes.

### **Priority Scheduling**

- Proportional Differentiated Services
  - Split traffic into "paid" and "unpaid" classes
  - Prioritize classes using quality differentiation parameters  $p_i$  and quality measure Q (EWMA)

 $p_1/p_2 = Q_1(\Delta t) / Q_2(\Delta t)$ 



#### Bank secrecy (honest-but-curious)

- Clients oblivious to  $x_r^d$ .
- B cannot produce r, input x, or output f<sub>r</sub>(x).
- Relay purchases are batched, preventing bank from knowing when prioritized circuits are constructed.

c and B evaluate  $f_r(x)$ 

- 1. c obtains  $bx_r^d$ .
- 2. c sends  $b H(x)x_r^d$  to B.
- 3. B sends  $H(H(x)x_r^d)$  to c.
- 4. c outputs  $H(x(H(H(x)x_r^d)))$ .

#### **PRF** Protocol

### Creating winning tickets

- $f_r$  is random in ROM when  $x_r^d$  unknown.
- $y_0 XOR y_1$  is random. for  $y_0$  or  $y_1$  unknown
- One-time-use inputs to f<sub>r</sub> prevent double spending.
- Tickets not fully purchased win with probability *p*.

$$f_r(x) = \mathsf{H}(x(\mathsf{H}(\mathsf{H}(x) \; x_r^{d})))$$

$$y_0 = f_r(x_1) \bigoplus x_0$$
  

$$y_1 = f_r(y_0) \bigoplus x_1$$
  

$$g_r(x) = y_0 \parallel y_1$$

$$0 \leq y_0 \oplus y_1$$

Cryptographic Lottery