

# Decentralized Anonymous Credentials

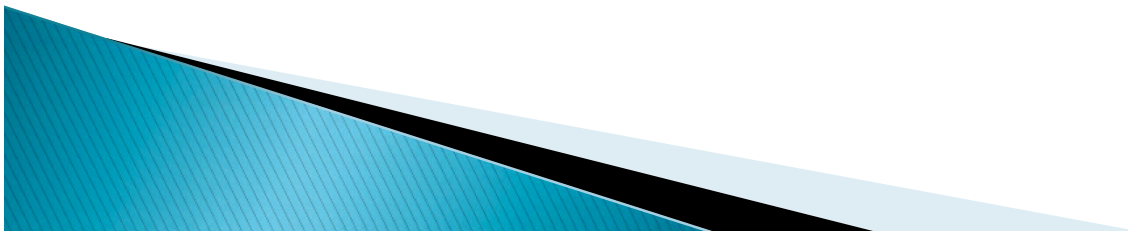
Christina Garman, Matthew Green, Ian Miers  
Johns Hopkins University



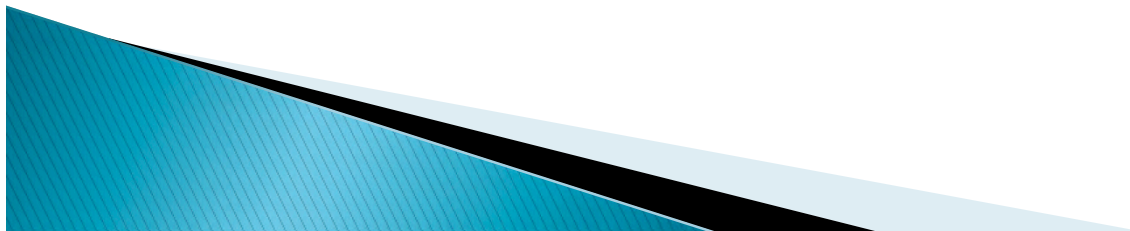
JOHNS HOPKINS  
UNIVERSITY

# Privacy and Identity on the Internet

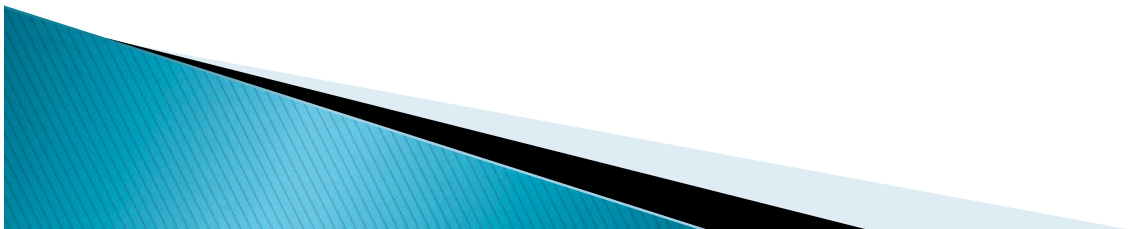
- ▶ Cannot make statements of identity privately
- ▶ But what about identity attributes?



# Privacy and Identity on the Internet



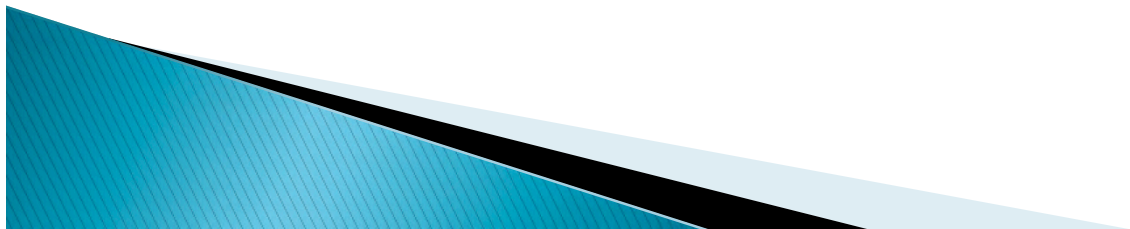
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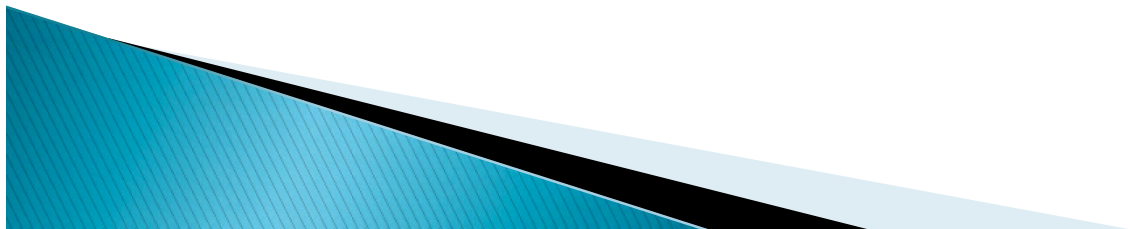
# Privacy and Identity on the Internet



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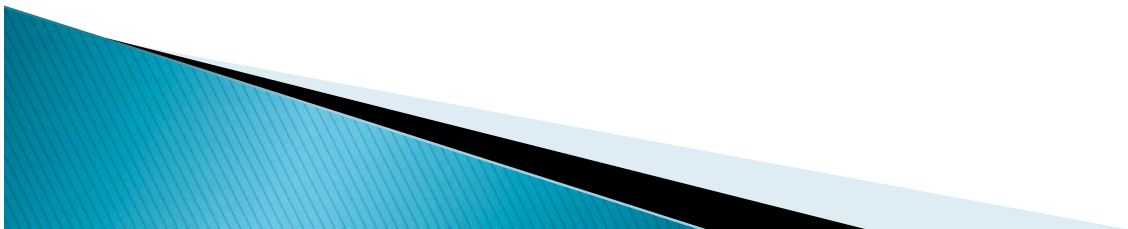
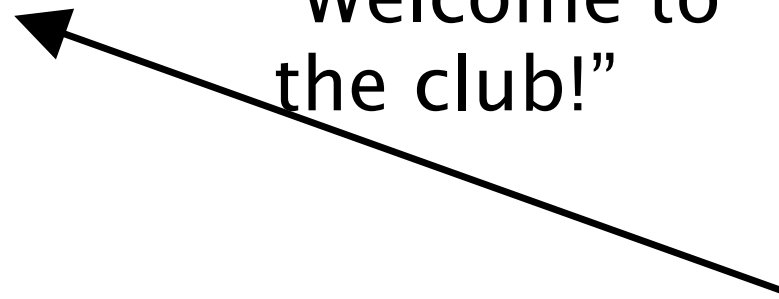
# Privacy and Identity on the Internet



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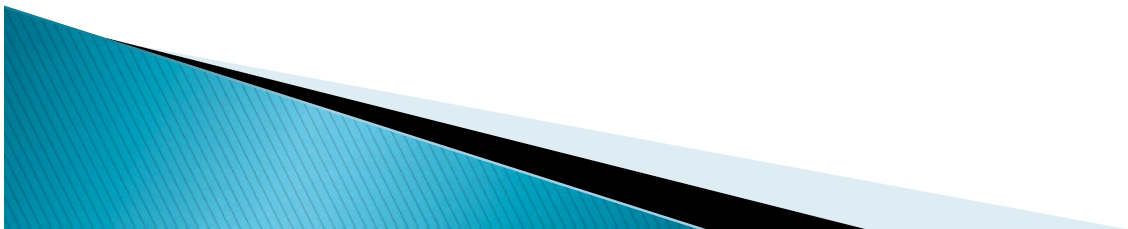
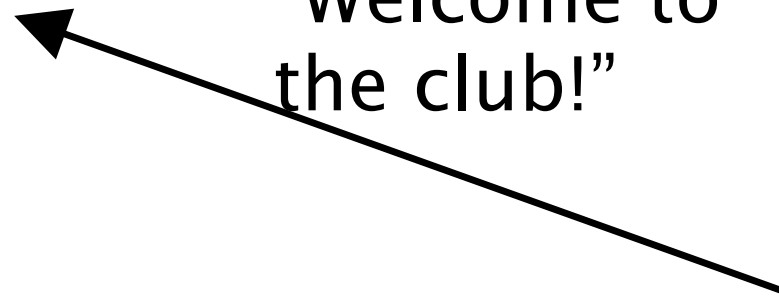
“Welcome to the club!”



# Privacy and Identity on the Internet



“Welcome to the club!”





# Privacy and Identity on the Internet



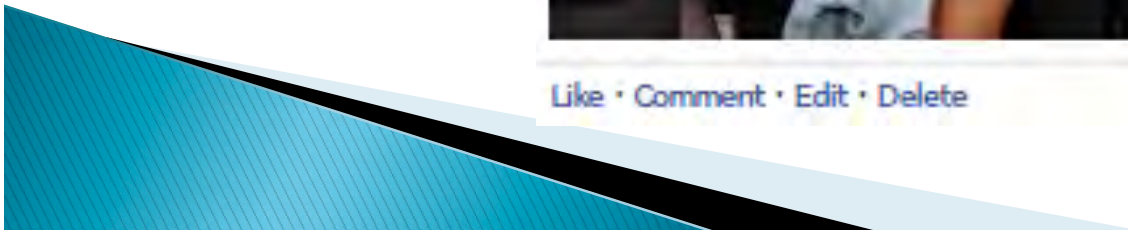
**Keith Alexander**

earlier today....

Keith liked the Justin Bieber Fan Club.

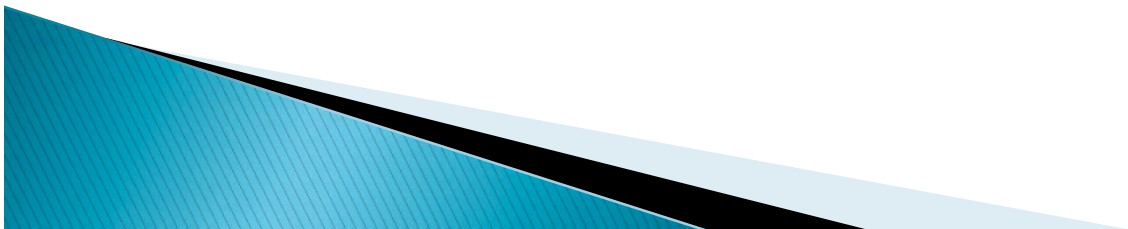


Like • Comment • Edit • Delete

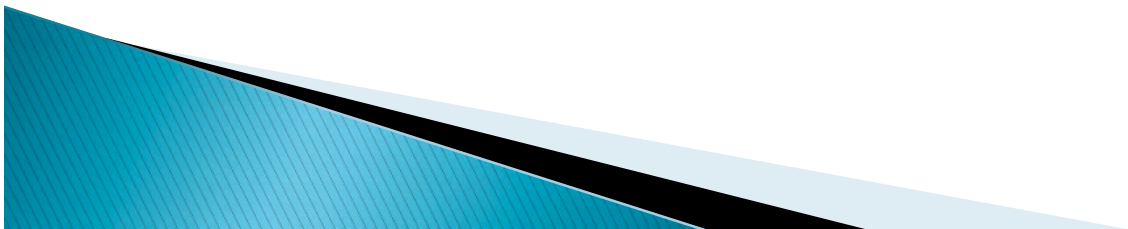


# Anonymous Credentials

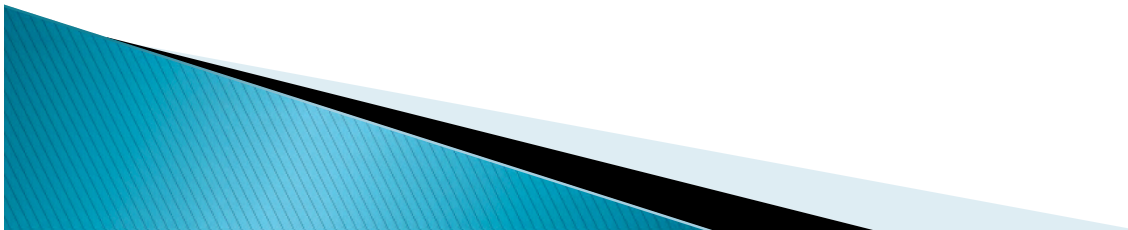
- ▶ Introduced by Chaum [Chaum85] and extended in [Brands00, CL01, CL02, CL03, BCKL08,...]
- ▶ Prove that you have a credential issued by some organization without revealing anything other than that you have the credential
- ▶ Standard techniques use a specialized digital signature



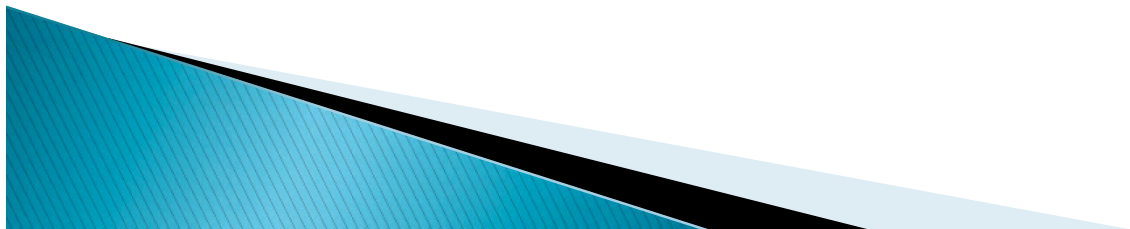
# Example of Anonymous Credentials



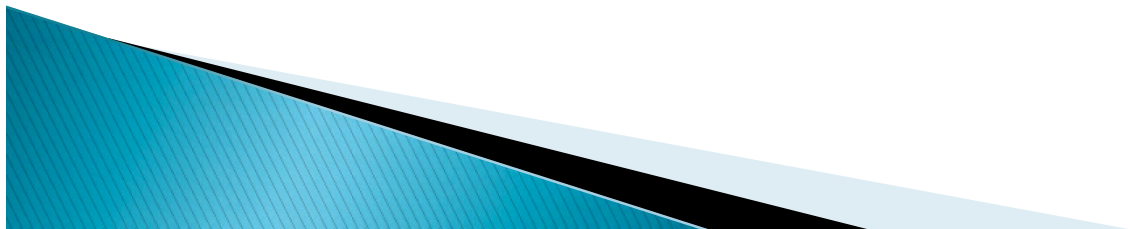
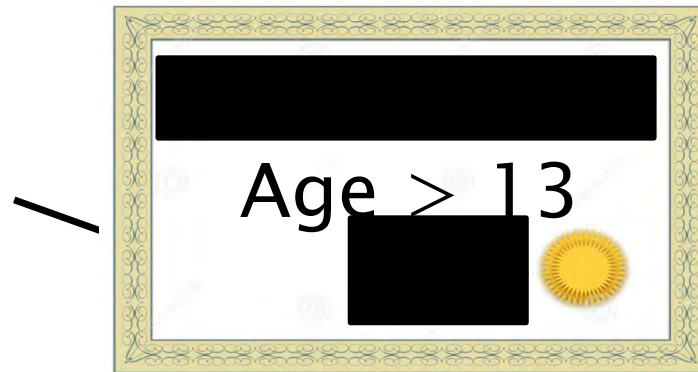
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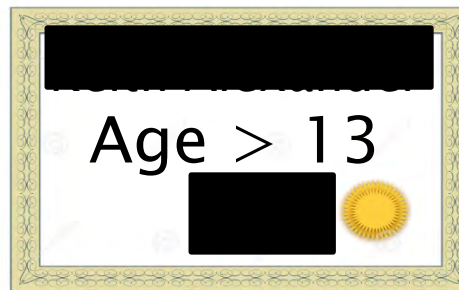
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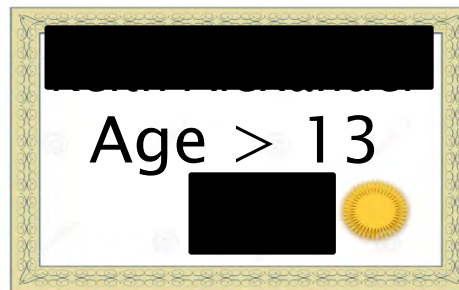
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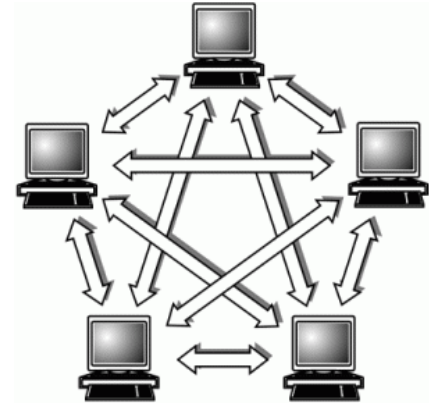
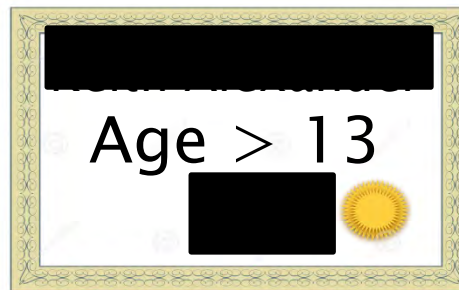


# Problems?



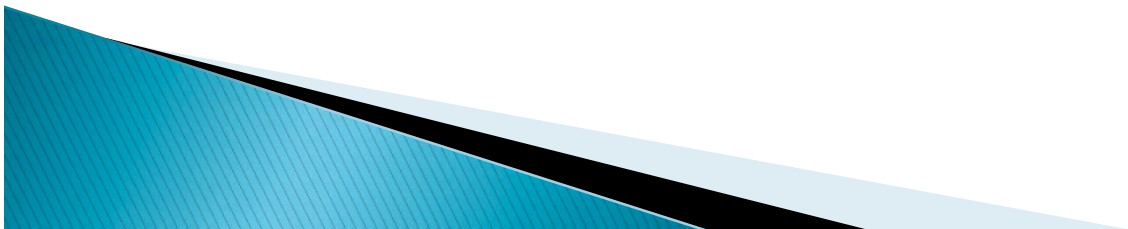


# Solution?



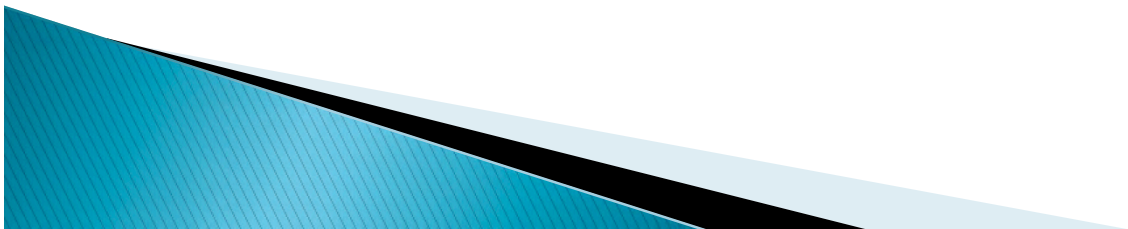
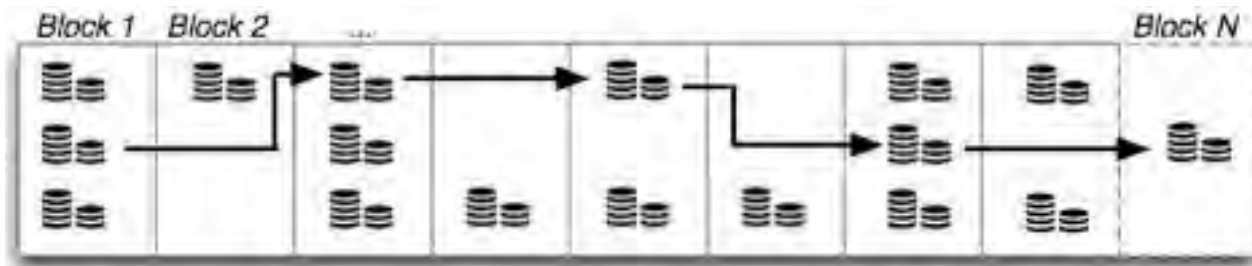
# Our Contribution: Decentralized Anonymous Credentials

- ▶ Related to our electronic cash proposal [MGGR13]
  - Zerocoin (decentralized e-cash)
- ▶ **Decentralized anonymous credentials**
  - Decentralized credential issuance
  - Decentralized identity certification
  - Requires:
    - Public append-only ledger
    - Publicly verifiable identity claims



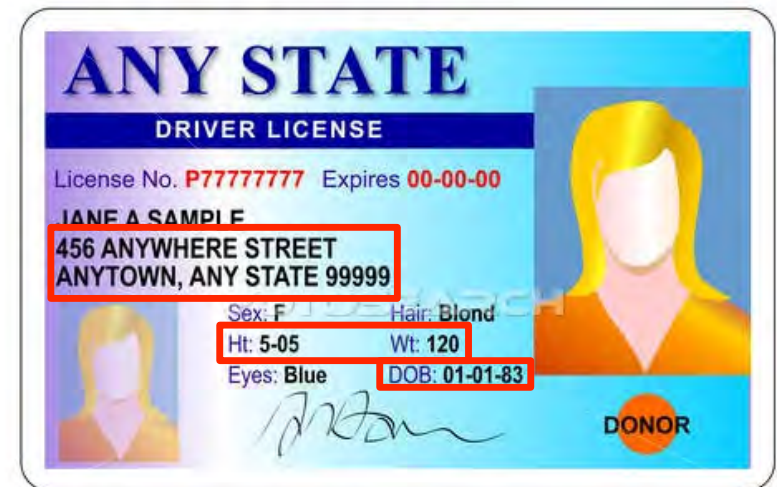
# Public Append-Only Ledger

- ▶ Central ledger (audited by users)
- ▶ Broadcast networks
- ▶ Distributed consensus network
  - Bitcoin block chain

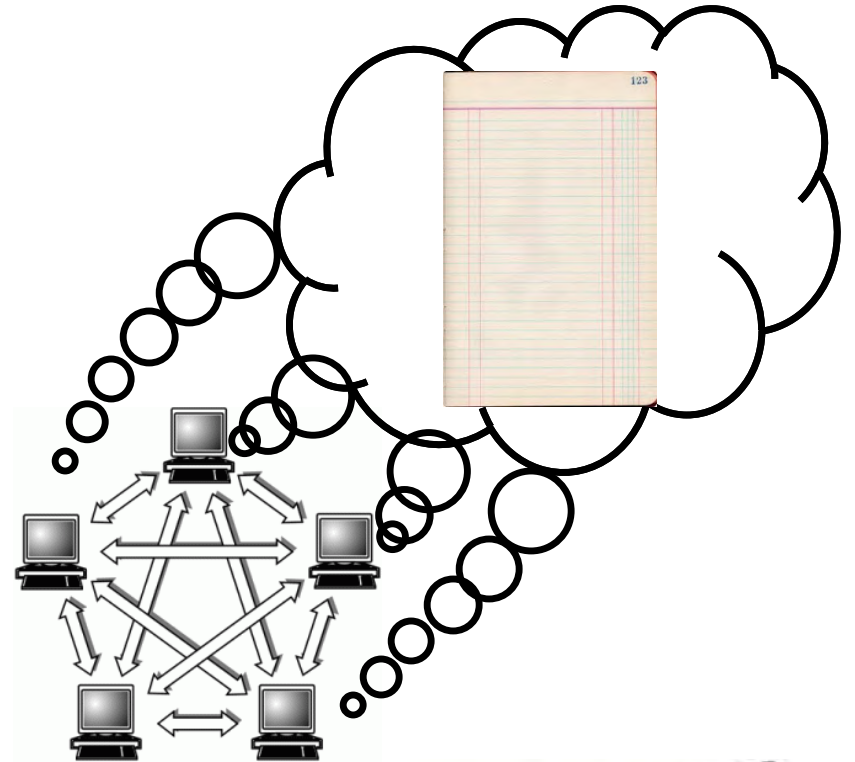


# Publicly Verifiable Identity Claims

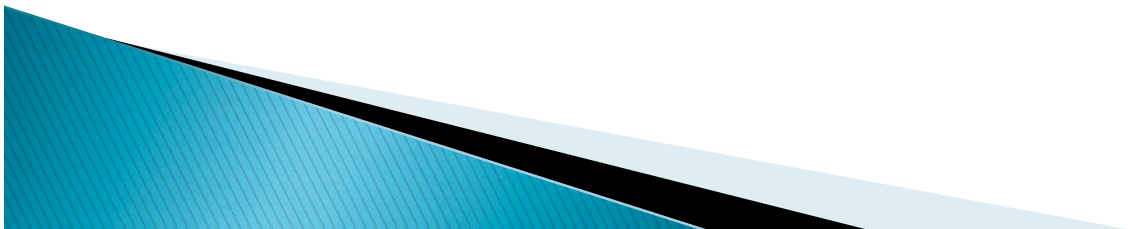
- ▶ Identity assertions are frequently publicly verifiable
- ▶ So why bother with (decentralized) anonymous credentials?
- ▶ Just because an identity assertion is publicly verifiable does not mean we want to link all of the information to every interaction!



# Overview



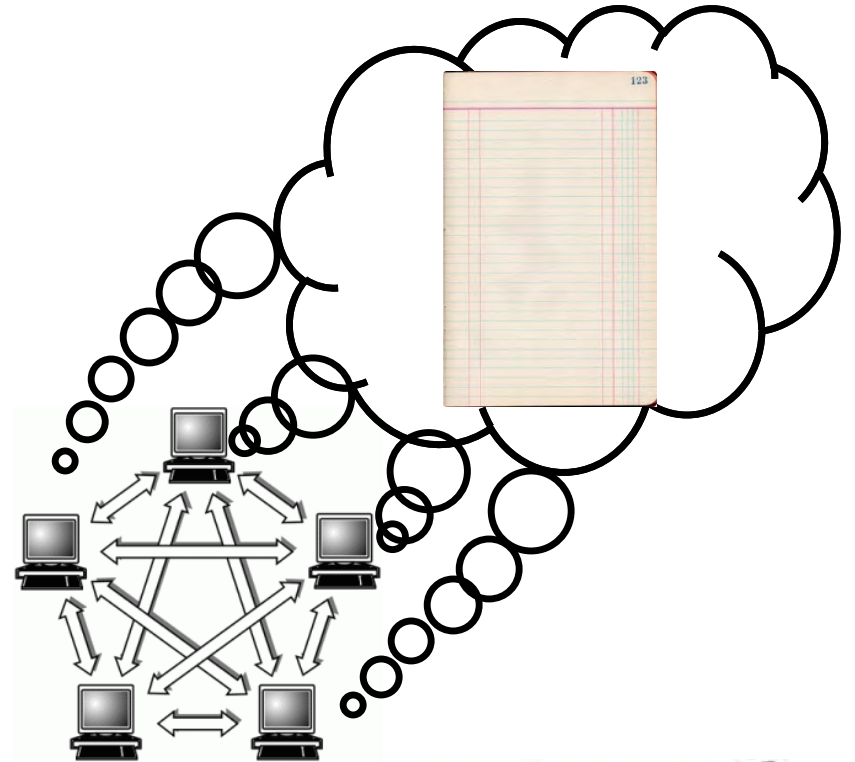
**JUSTIN BIEBER  
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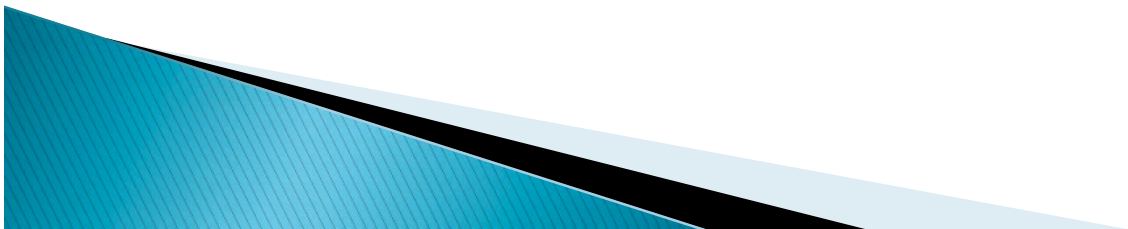
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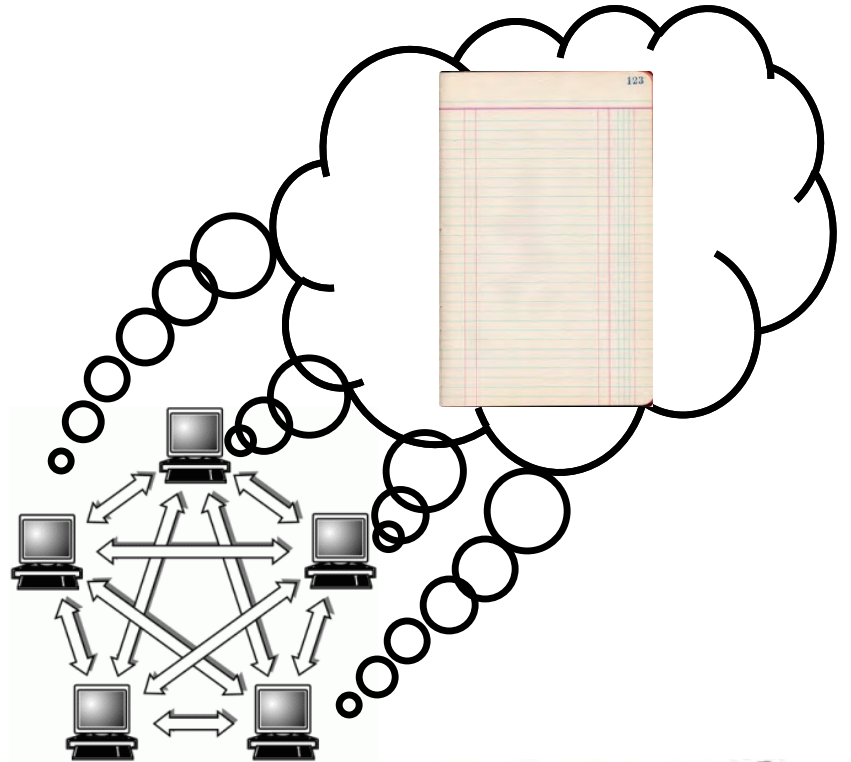
*cred*



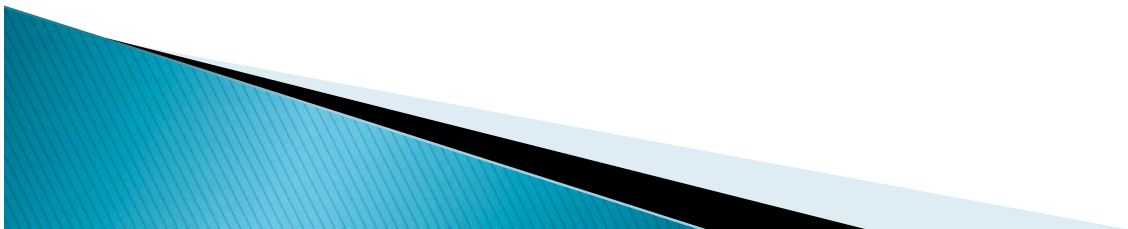
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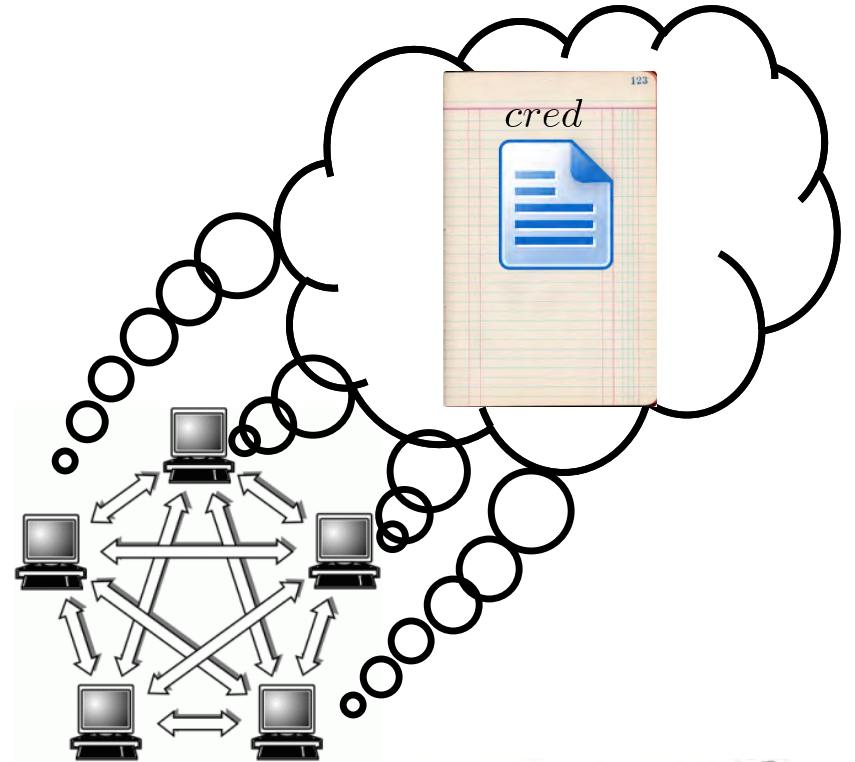
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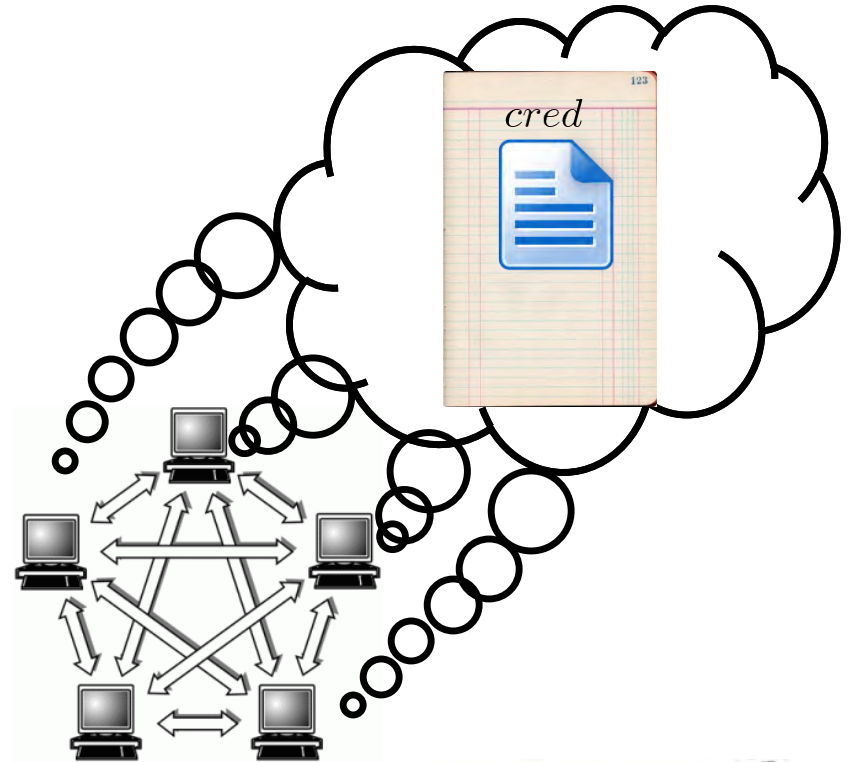


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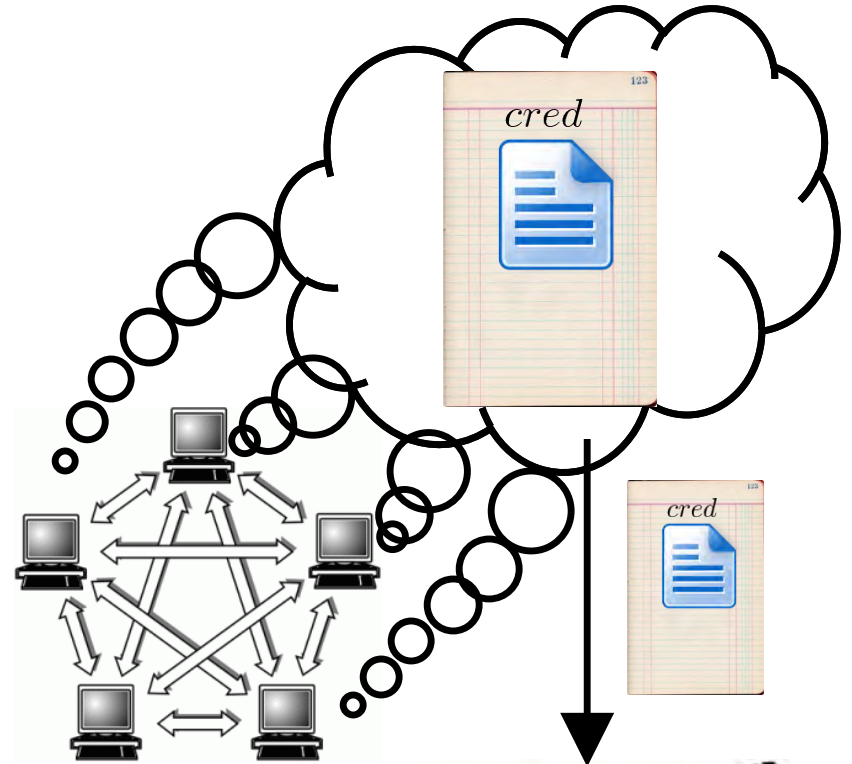
# Overview



“A credential  
on the ledger  
says age > 13.”



# Overview



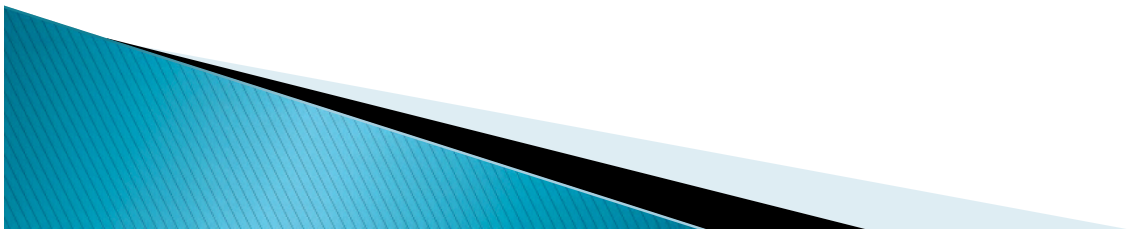
“A credential on the ledger says age > 13.”

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# Cryptographic Building Blocks

- ▶ Commitments
- ▶ Zero-knowledge proofs
- ▶ Accumulators



# Commitments

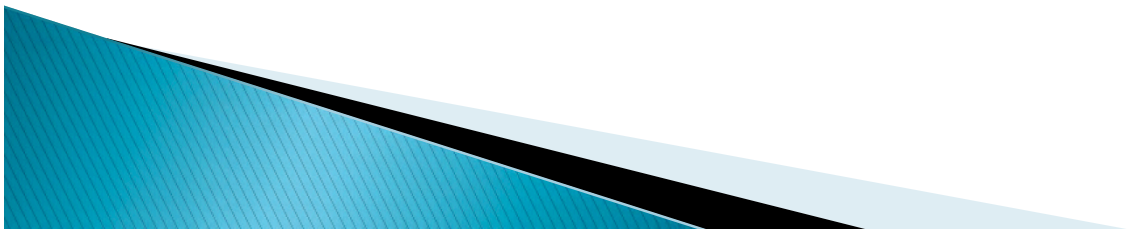
- ▶ Allow you to commit to and later reveal a value
- ▶ Binding: value cannot be tampered with
- ▶ Hiding: value cannot be read until revealed
- ▶ We use Pedersen commitments

$$C = g^x h^r \text{ mod } q$$



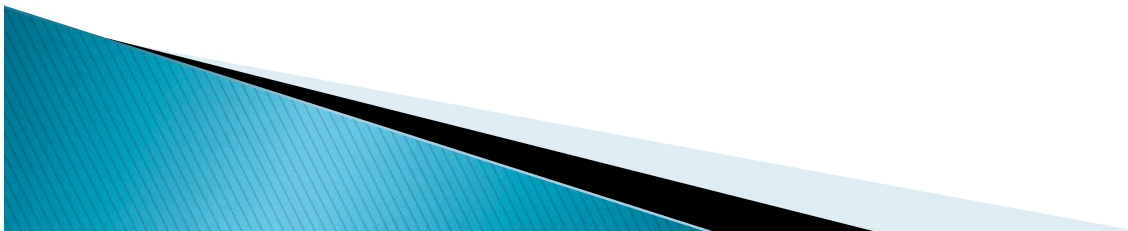
# Zero-knowledge Proofs

- ▶ Zero-knowledge [Goldwasser, Micali 1980s, and beyond]
- ▶ Prove a statement without revealing any other information
- ▶ Specific variant: non-interactive proof of knowledge
- ▶ Here we prove we know:
  1. The opening for a credential
  2. That the credential is in the ledger



# An inefficient approach...

- ▶ Inefficient proof
  - Identify all valid credentials in the ledger (call them  $C \downarrow 1, \dots, C \downarrow N$ )
  - Prove that you know the opening of a credential  $C$  and  $C = C \downarrow 1 \vee C = C \downarrow 2 \vee \dots \vee C = C \downarrow N$
  - This “OR” proof is  $O(N)$



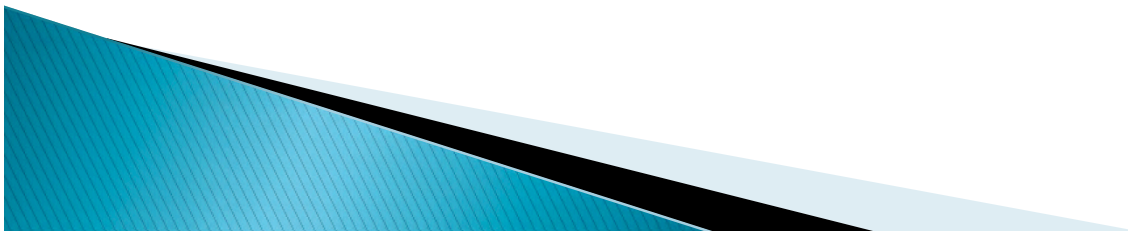
# Cryptographic Accumulators

- ▶ Allow constant size set membership proofs
- ▶ Strong RSA accumulator originally due to Benaloh and de Mare
- ▶ Efficient proof for accumulation of primes proposed by Camenisch and Lysyanskaya '01

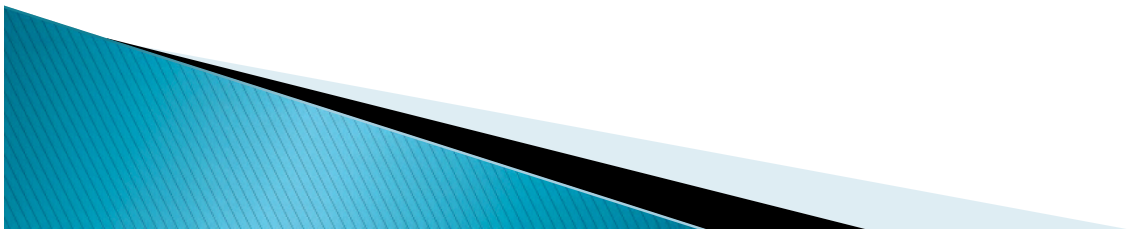
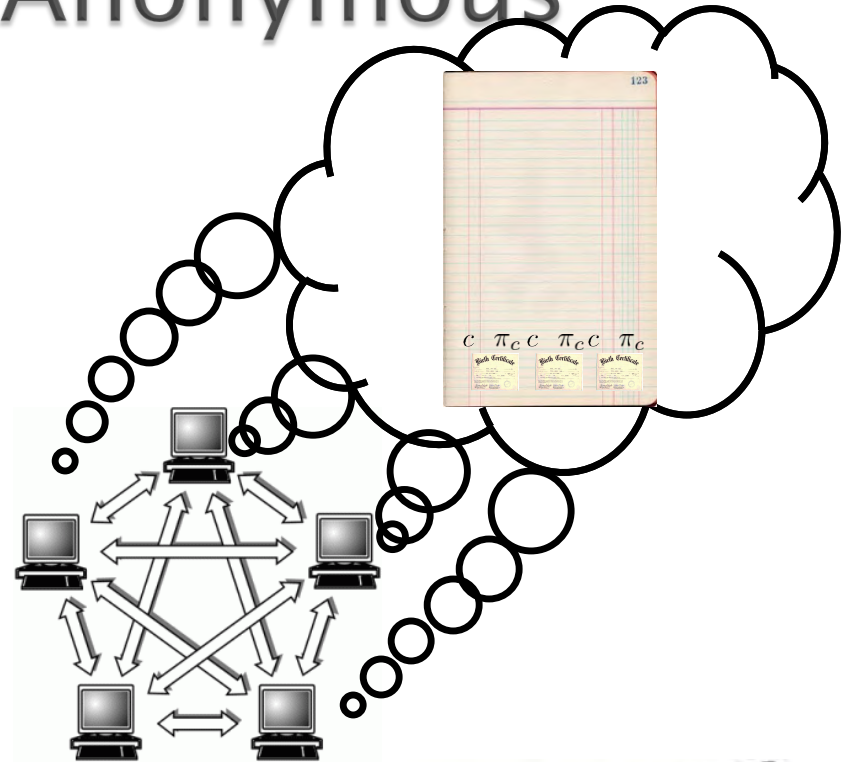
$$N = p \cdot q, u \in QR_N(u \neq 1)$$

$$A = u^{C_1 \cdot C_2 \cdot \dots \cdot C_n} \bmod N$$

$$w_i = u^{C_1 \cdot C_2 \cdot \dots \cdot C_{i-1} \cdot C_{i+1} \cdot \dots \cdot C_n} \bmod N$$



# Basic Decentralized Anonymous Credentials





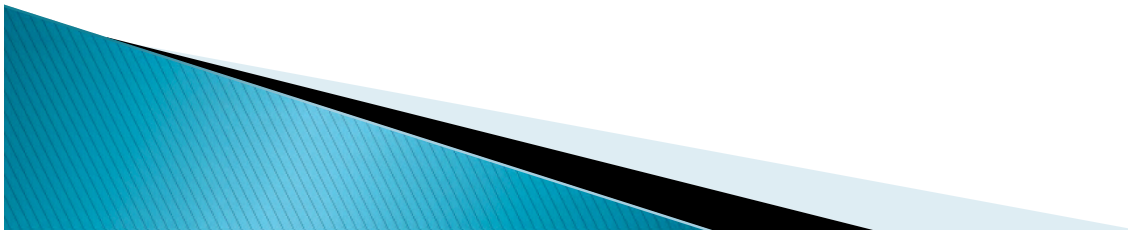
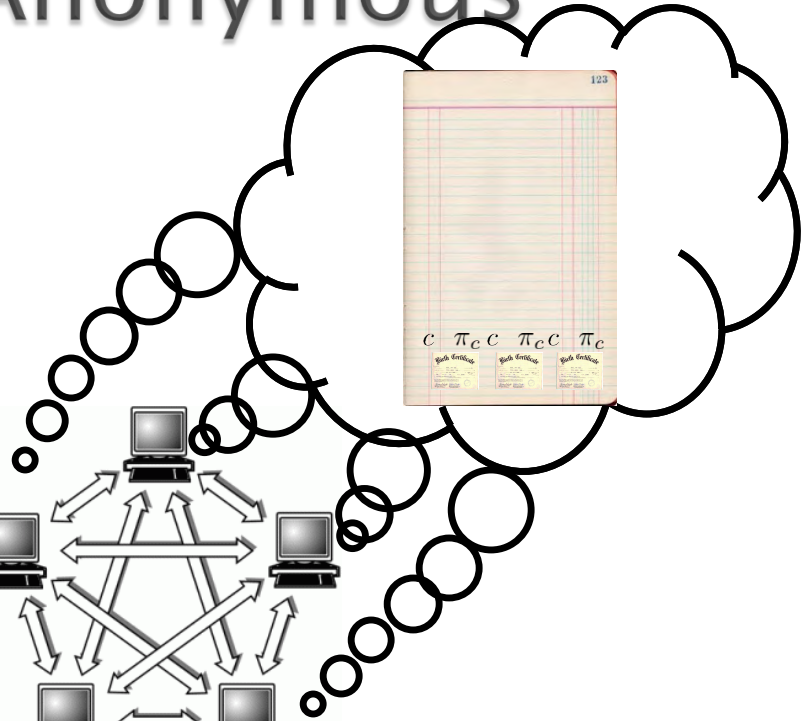
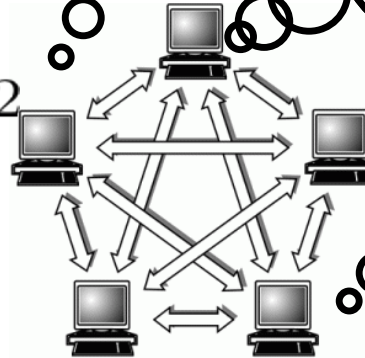
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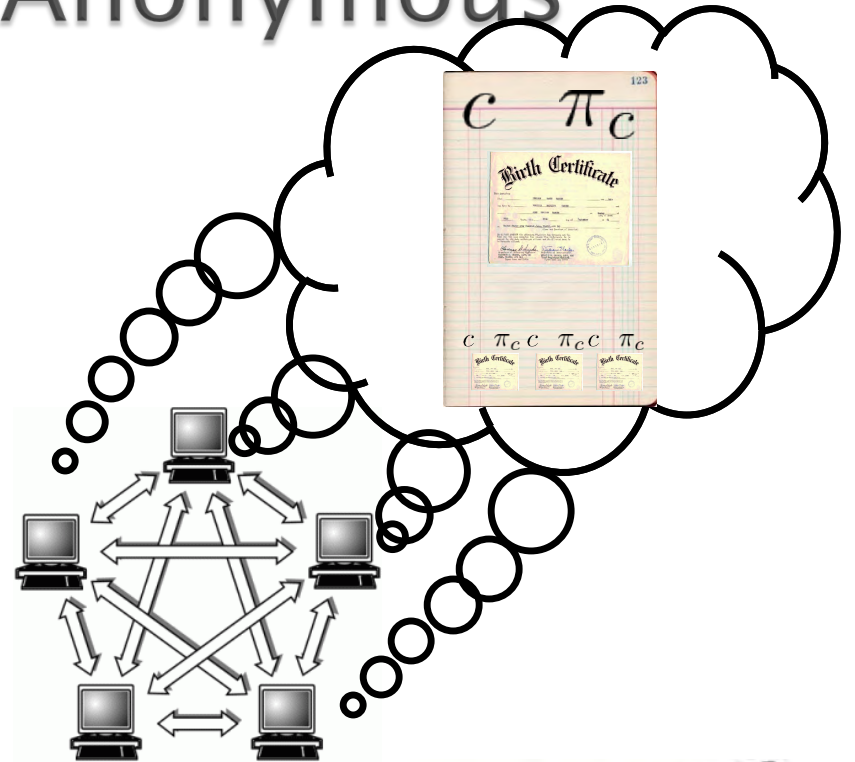
$$c = g_0^r g_1^{sk} g_2^{\text{age}=62}$$



$\pi_c$



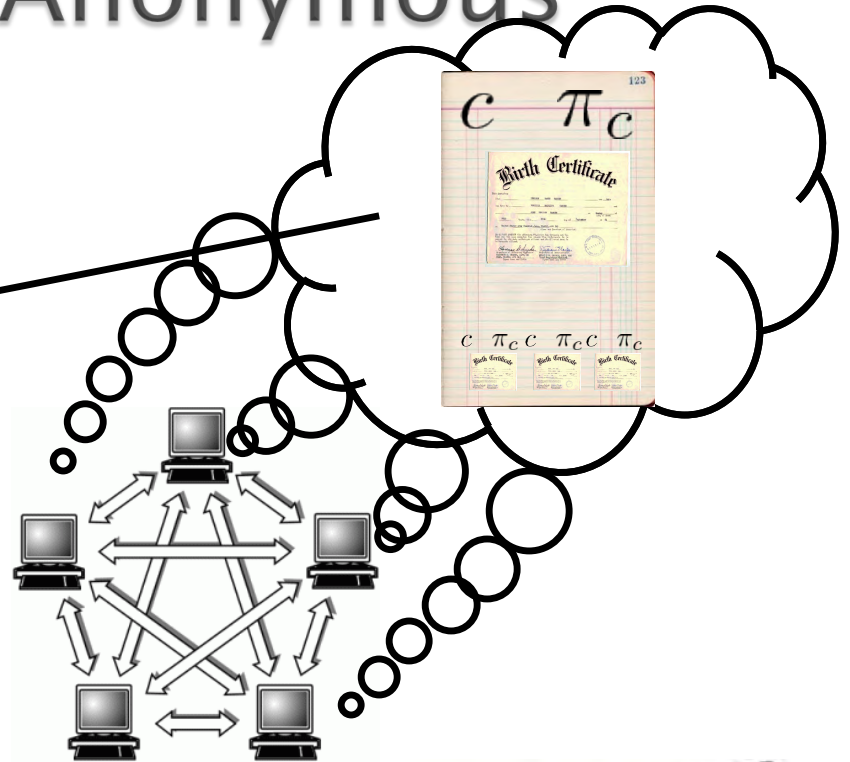
# Basic Decentralized Anonymous Credentials



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$c_1, c_2, \dots, c_n$

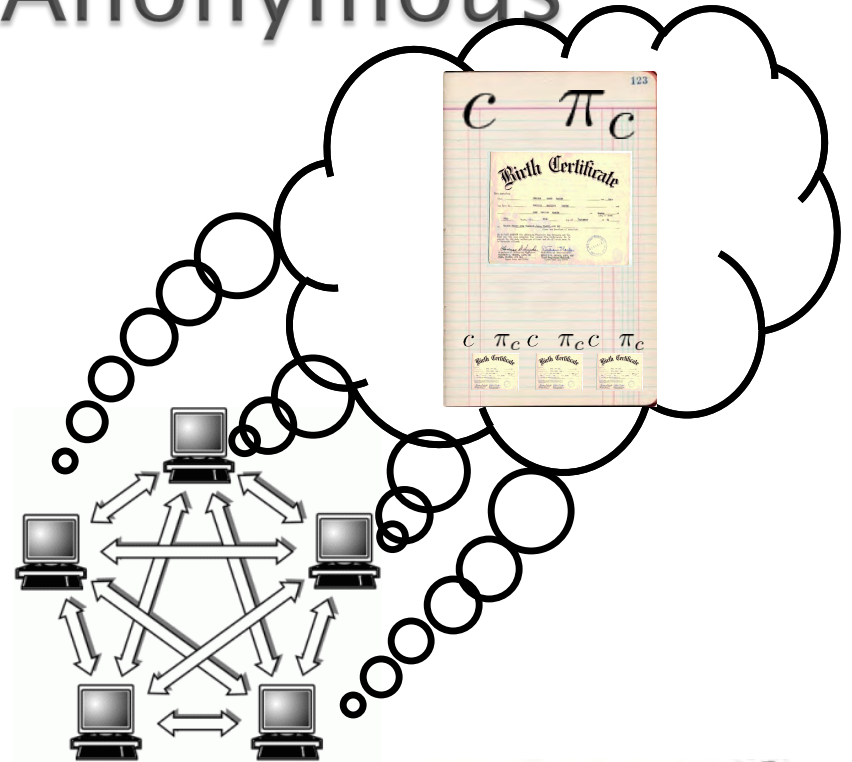


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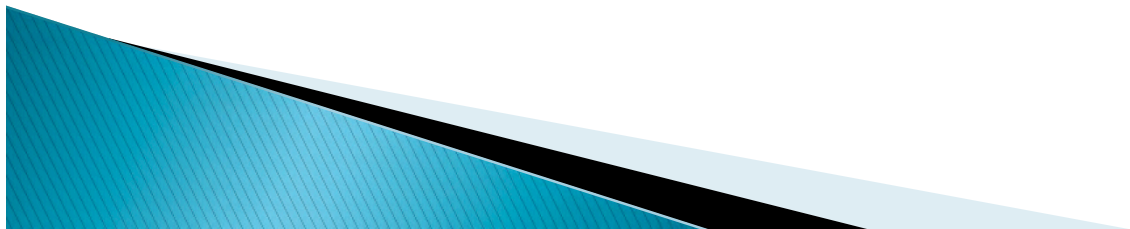
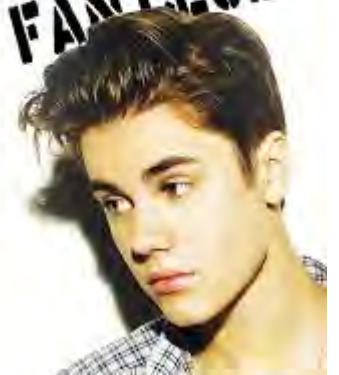


# Basic Decentralized Anonymous Credentials

$$A = u^{c_1 \cdot c_2 \cdot \dots \cdot c_n} \text{ mod } N$$

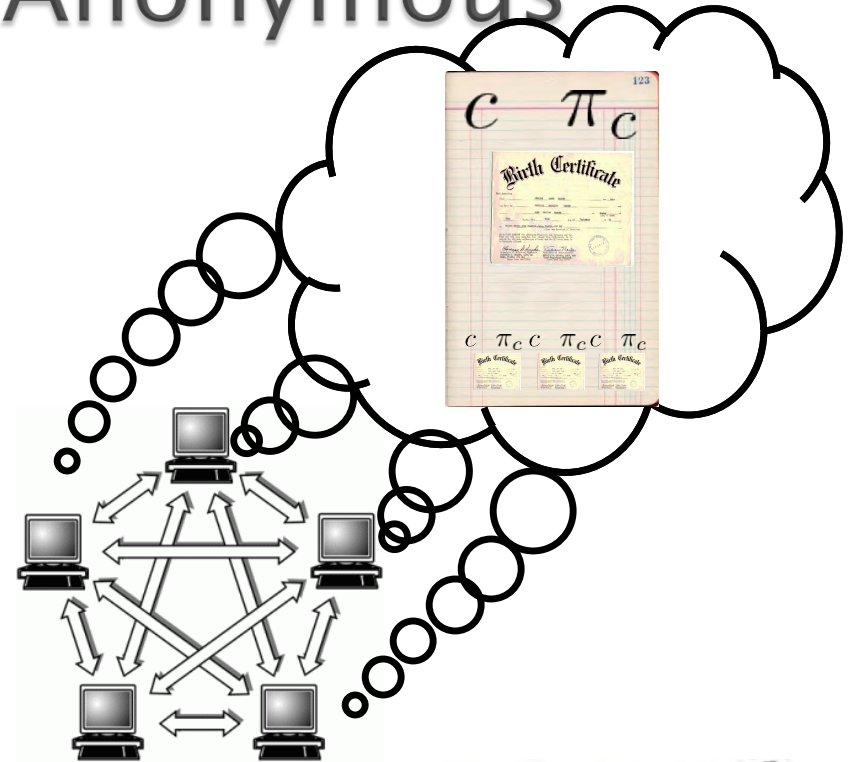


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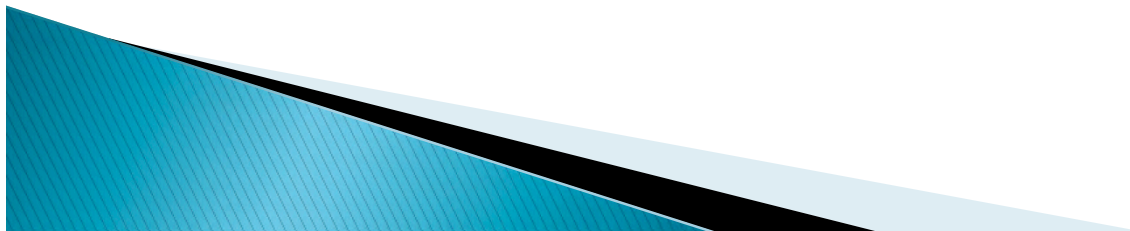
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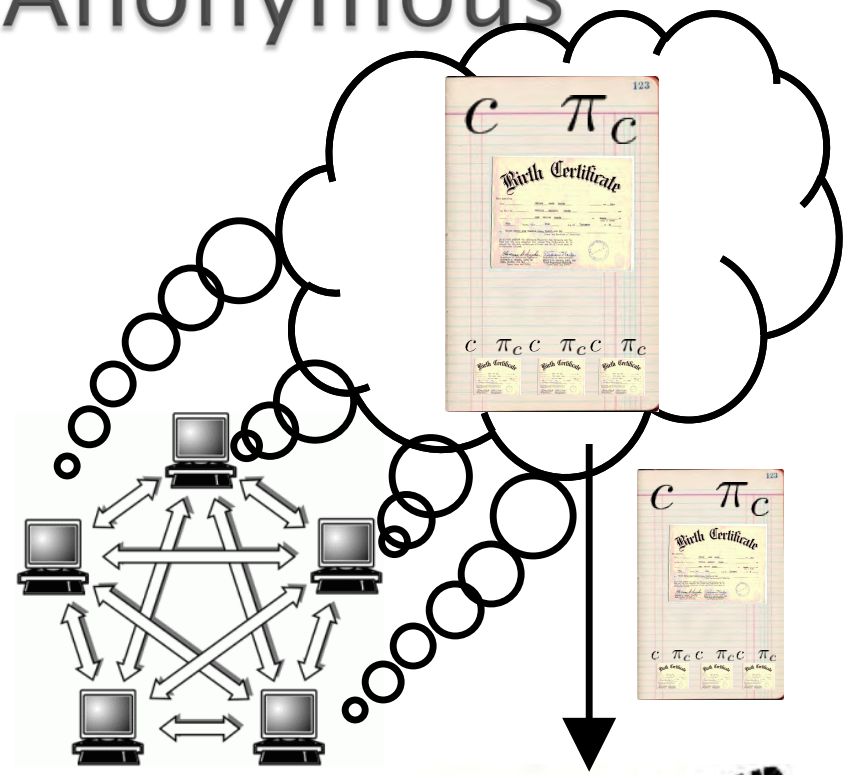
$\pi_s$

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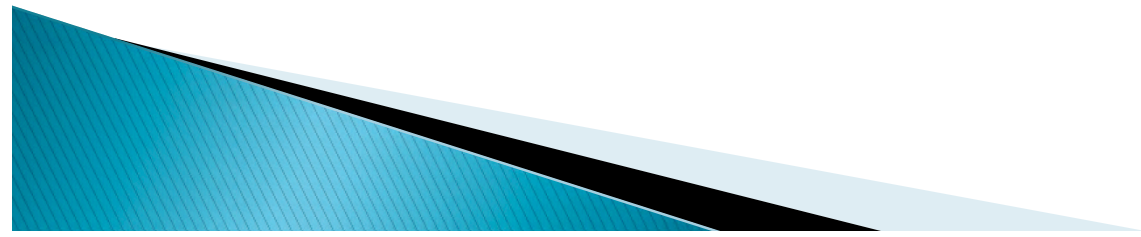
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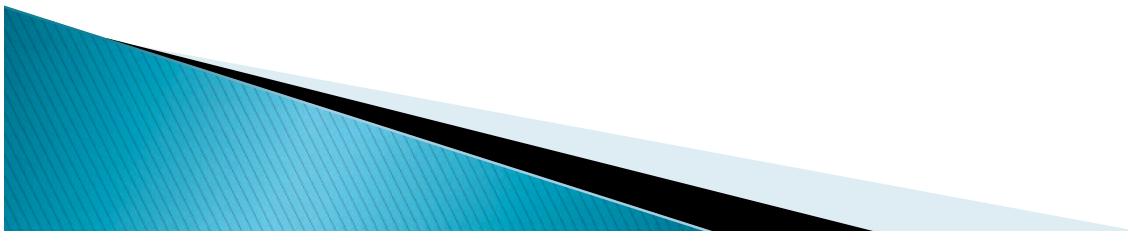
$\pi_s$

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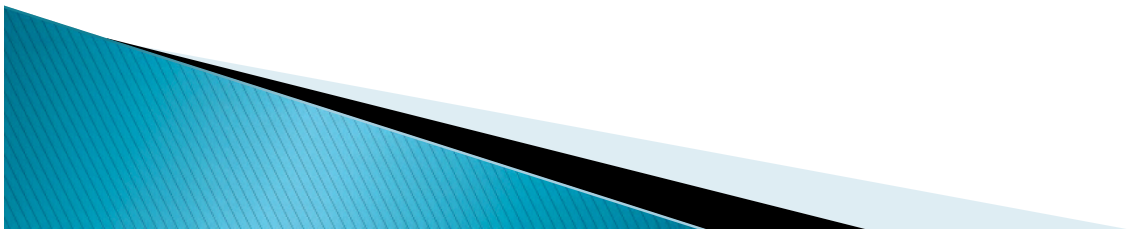
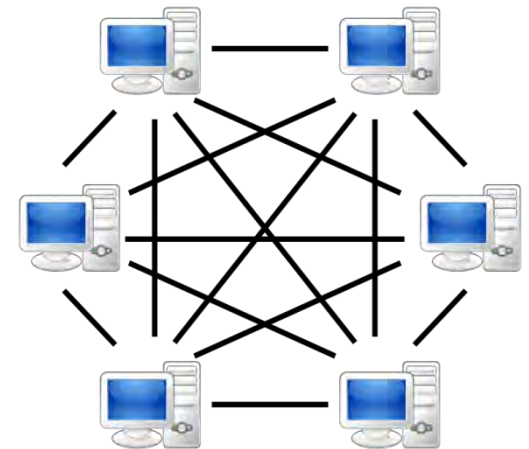


# Applications

- ▶ Anonymous resource management in ad hoc networks
- ▶ Decentralized Direct Anonymous Attestation
- ▶ Auditable credentials
- ▶ Mitigating Sybil attacks in ad hoc networks



# Protecting Against Sybil Attacks

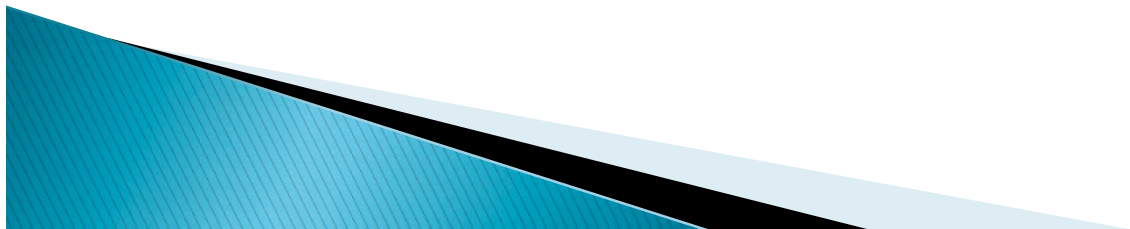
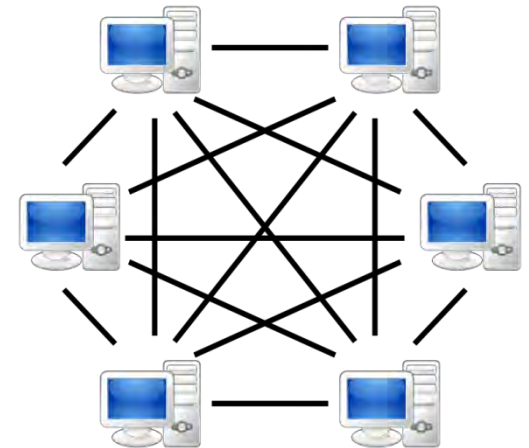




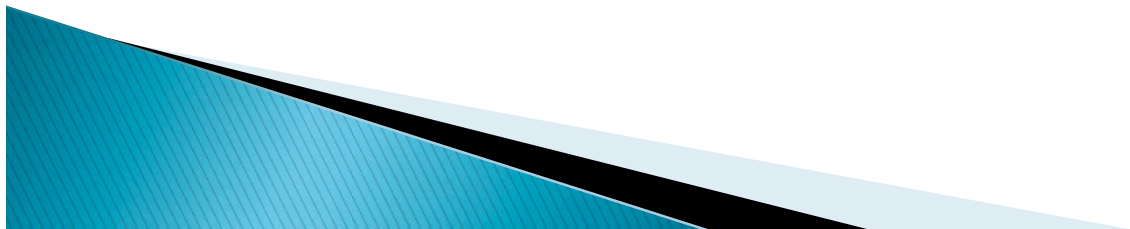
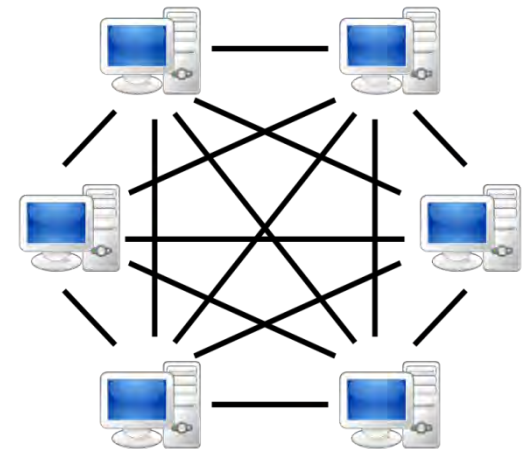
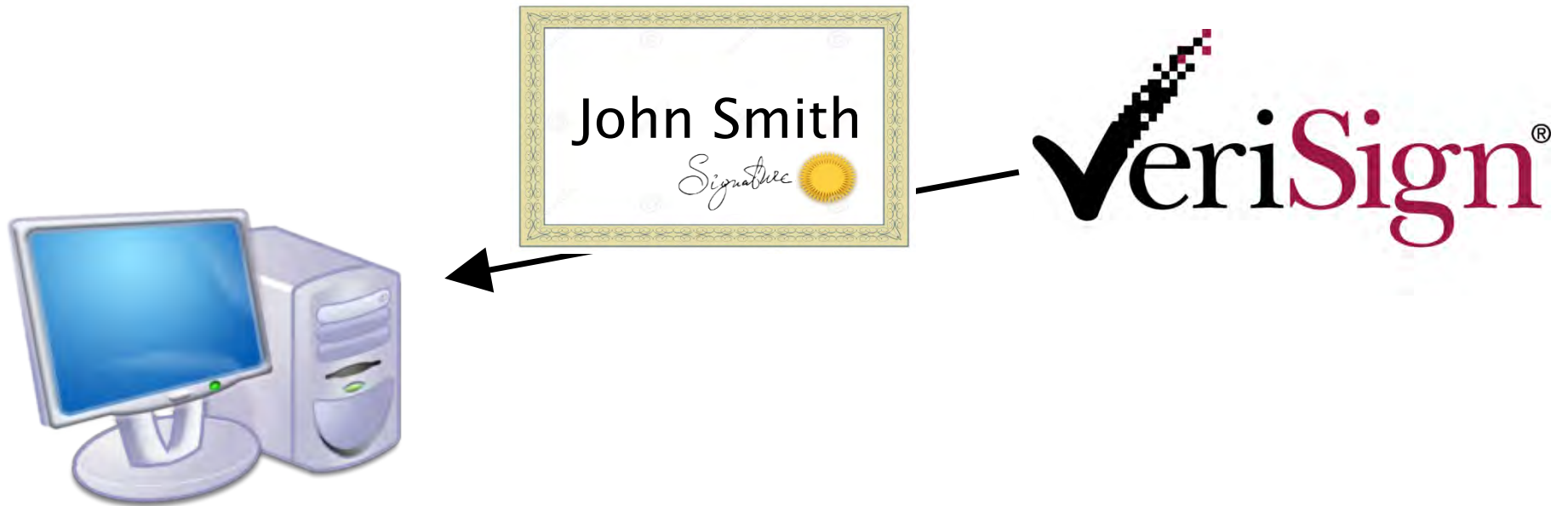
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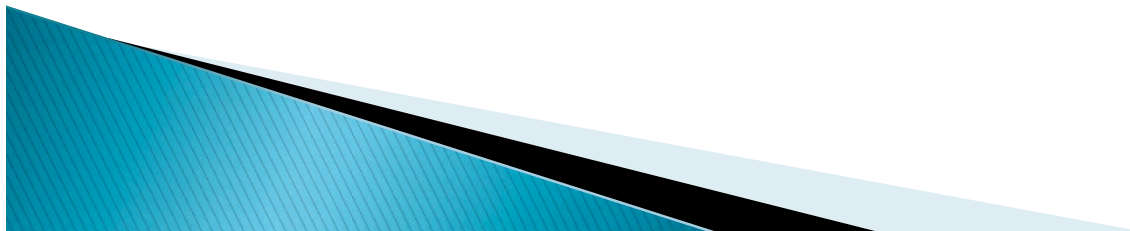
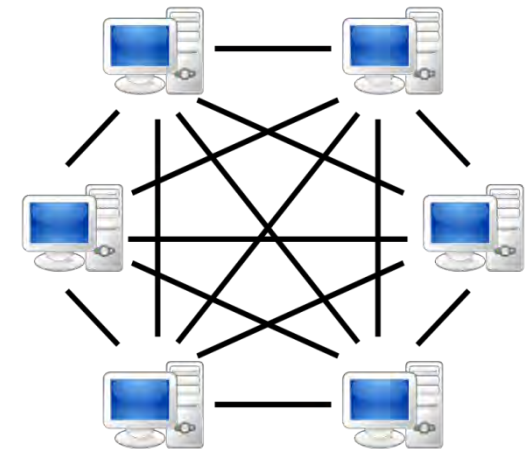
"I am John Smith", \$  
\$



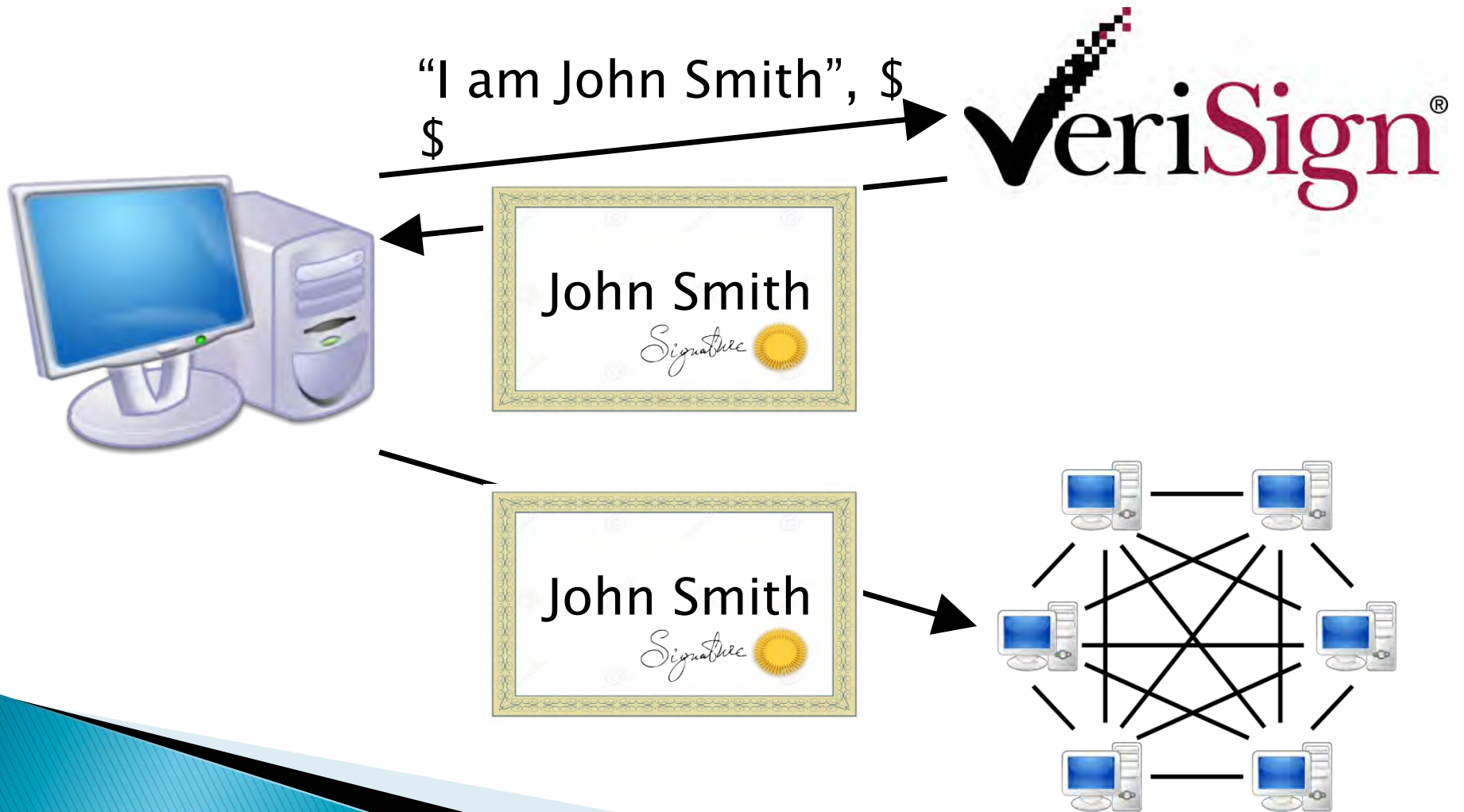
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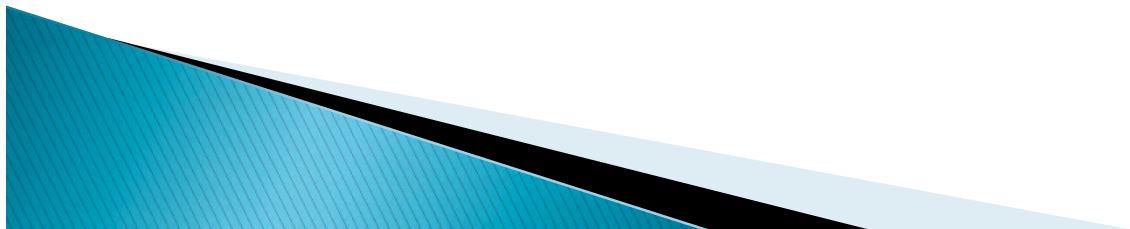
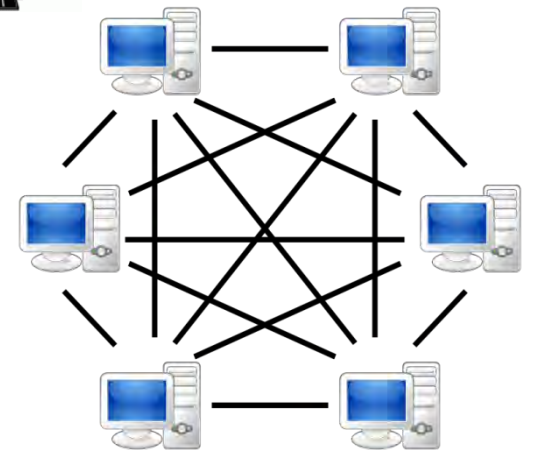
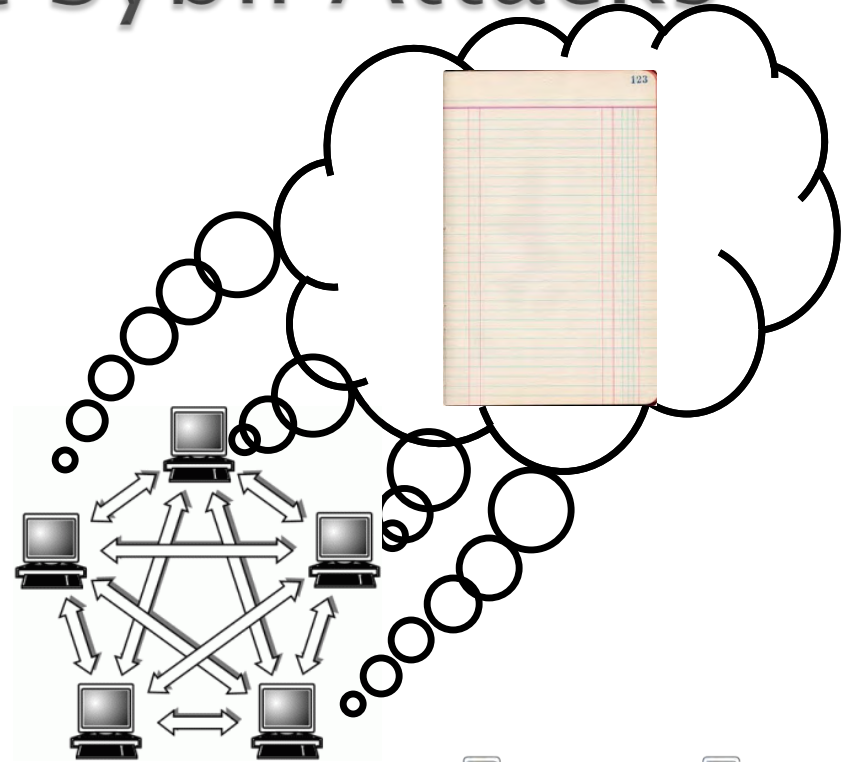
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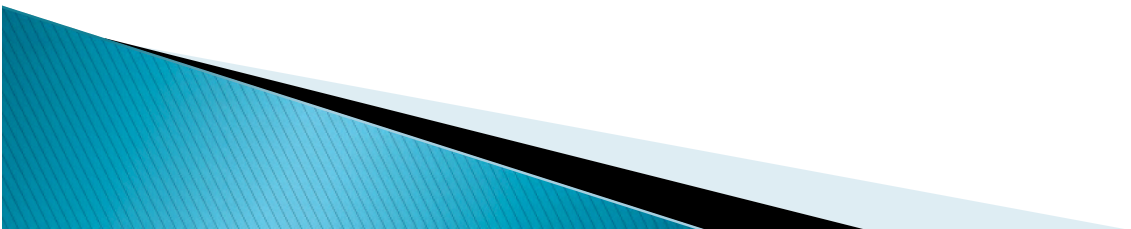
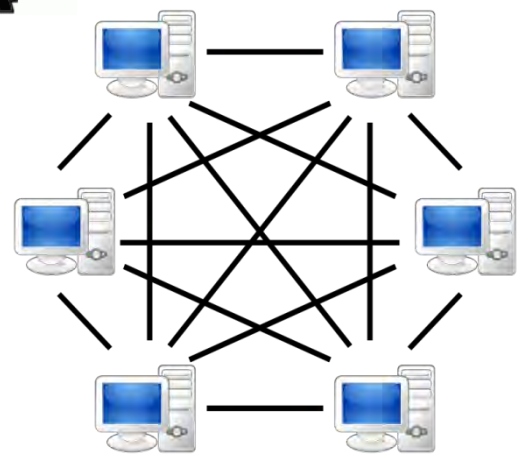
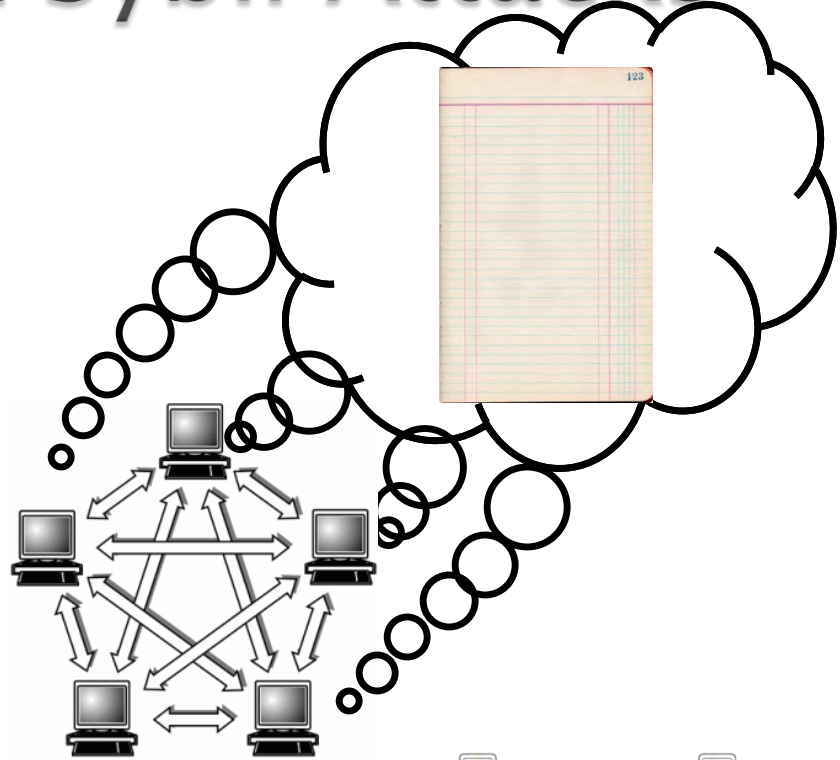
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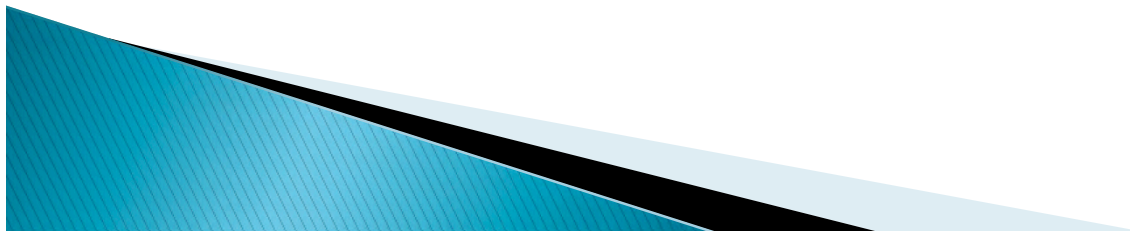
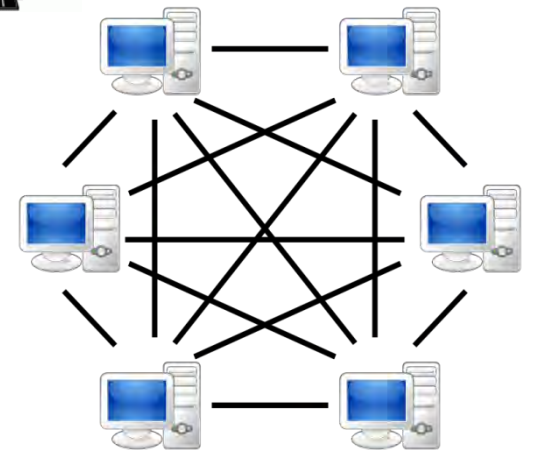
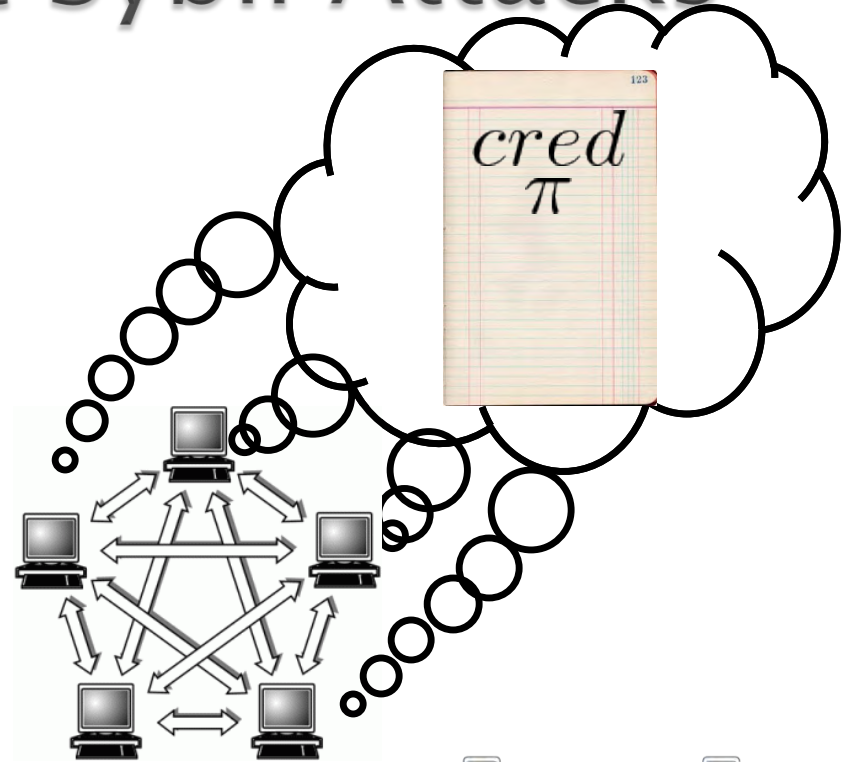
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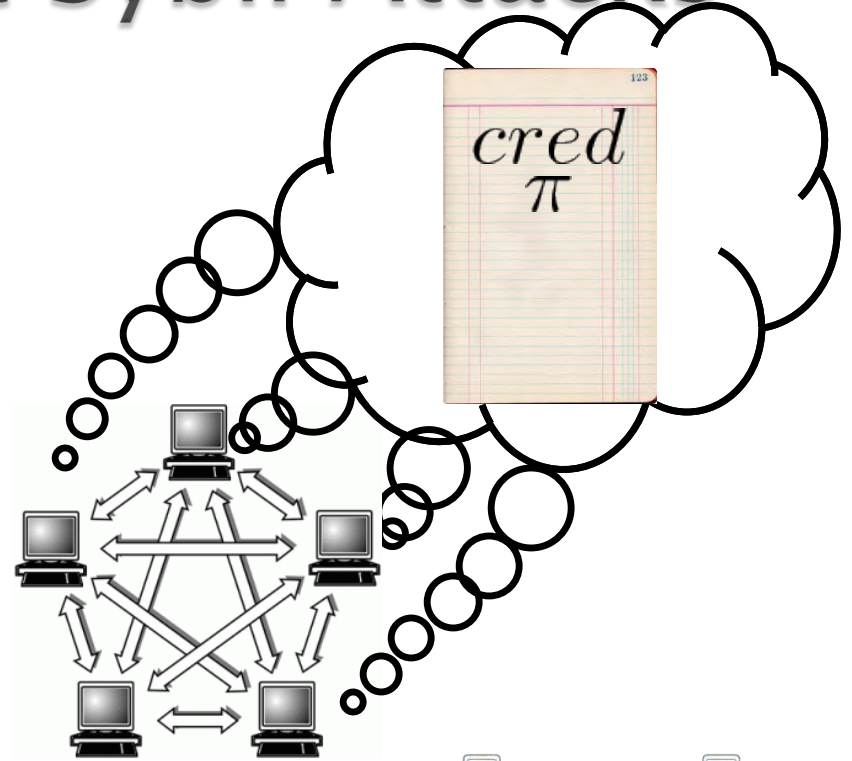
*cred*  
"I have paid  
1 BTC"



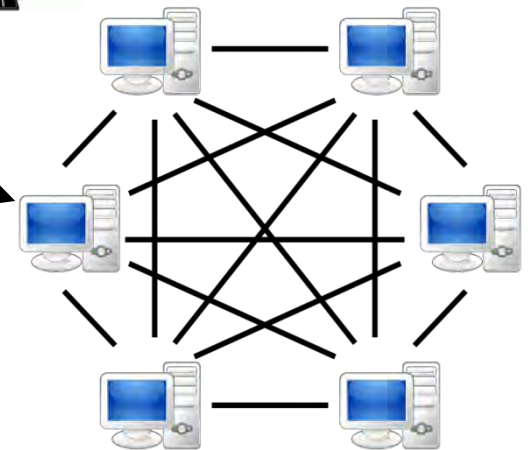
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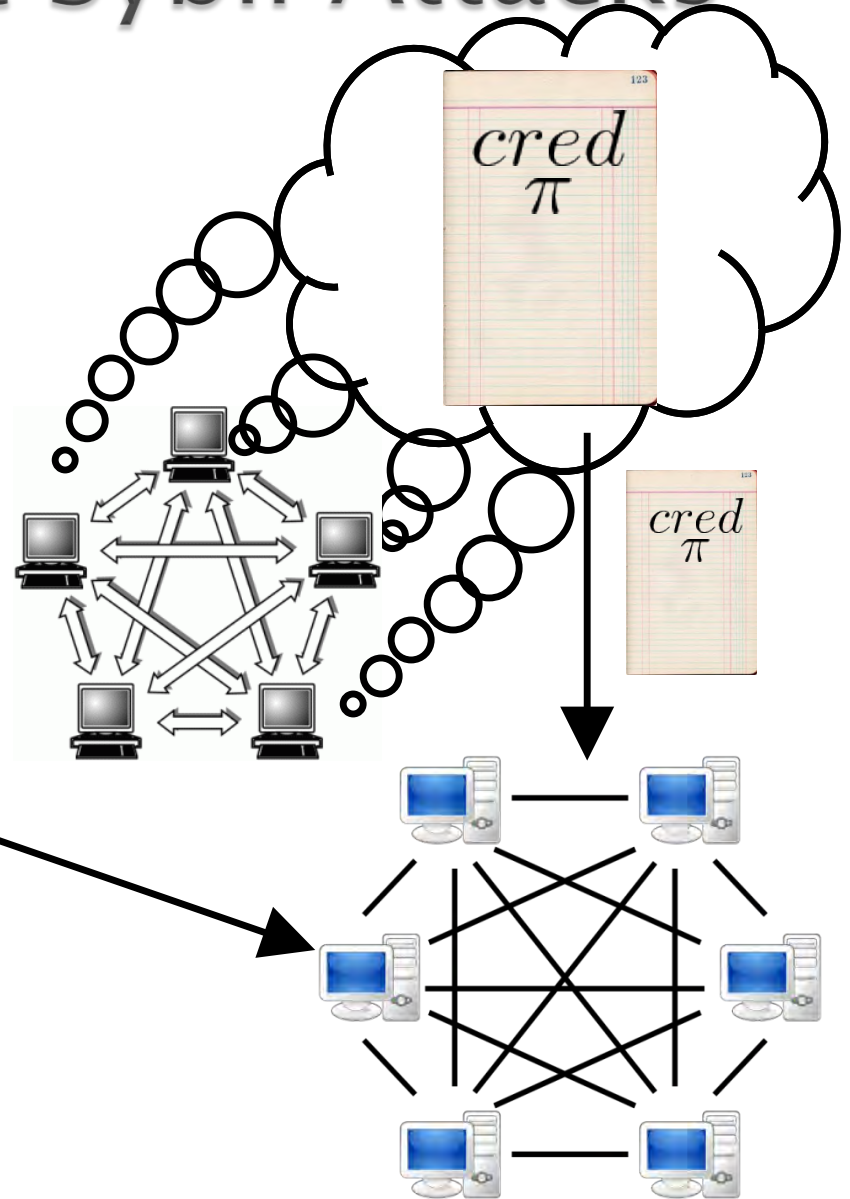


"I am not  
a Sybil"

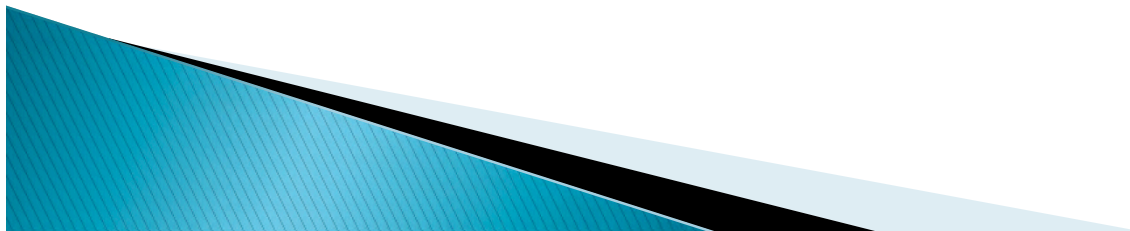




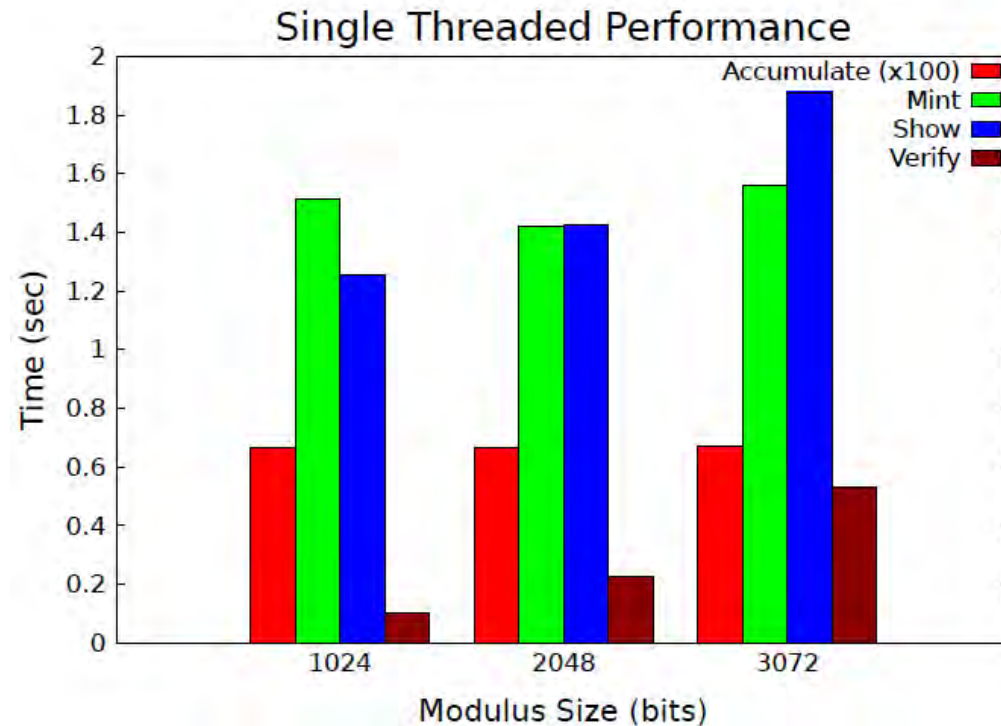
# Protecting Against Sybil Attacks



“I am not  
a Sybil”



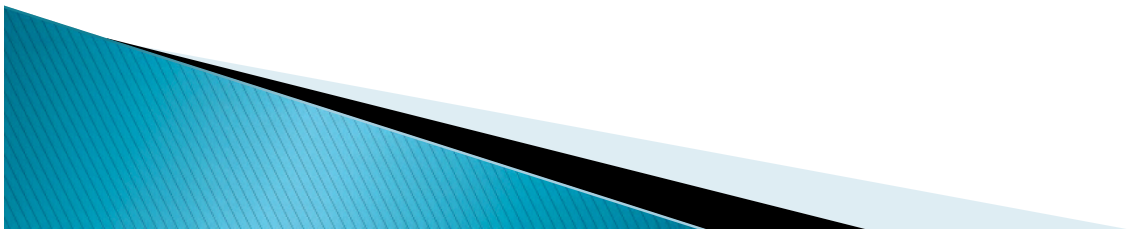
# Performance



- ▶ Basic scheme implemented as stand-alone library
  - Proofs 50 KB

# Future Work

- ▶ Better, smaller “proofs” of knowledge:
- ▶ Succinct Non-Interactive **AR**guments of Knowledge (zkSNARKs) [PHGR13, BCGTV13]
  - 288 byte proof for arbitrary-sized arithmetic circuits
  - 8 ms verification time
- ▶ Additional applications?



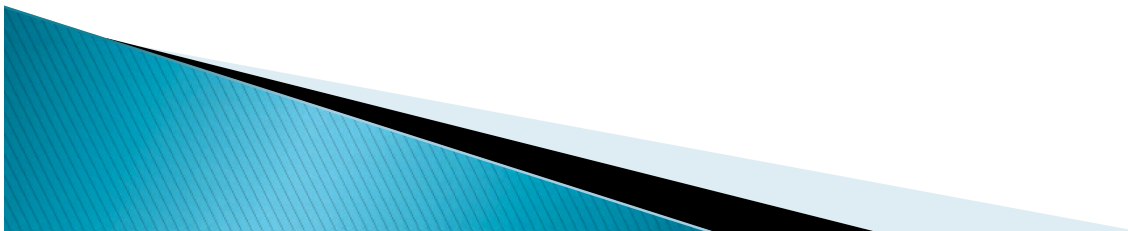
# Questions?



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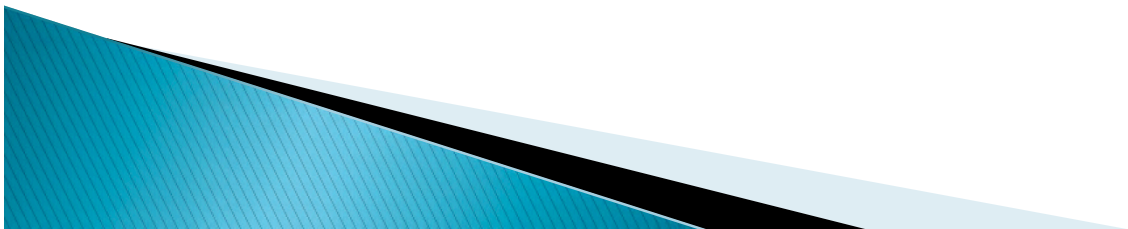
# Potential Alternatives

- ▶ Threshold cryptography
  - High setup cost for large number of parties
  - Difficult for parties to come and go
- ▶ Ring signatures [RST01]
  - Grow linearly with the number of participating signers
  - Expensive to generate



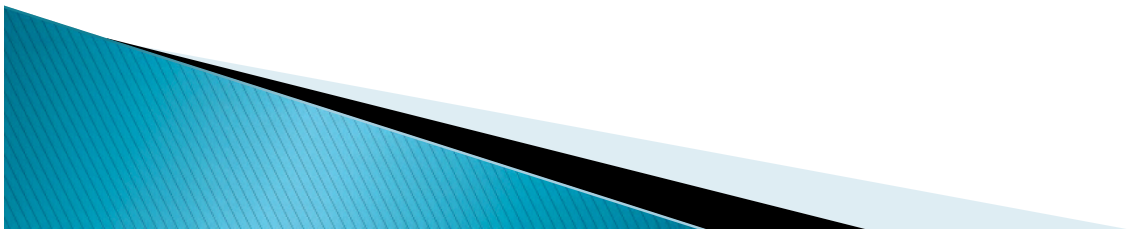
# Non Publicly Verifiable Credentials

- ▶ Credential transform service
- ▶ Allows user to transform a credential to an anonymous credential without additional trust assumption
- ▶ Works for any statement that an authority can certify



# Proof of Work for Sybil Attacks

- ▶ Proof of resource expenditure instead of payment
- ▶ Cannot reuse proof of work with different peers
  - Not anonymous
  - Clonable
- ▶ Do not want to have to do a proof of work with each peer in the system
- ▶ Instead do one proof of work per  $k$  interactions



# Resource Management

- ▶ Publicly verifiable proofs of resources
- ▶ File storage, bandwidth, etc.
- ▶ Do not want to link resources provided to resources consumed
  - Files uploaded vs. files downloaded

